

Misfit Layer Compounds: A Platform for Heavily Doped 2D Transition Metal Dichalcogenides

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Transition metal dichalcogenides (TMDs) display a rich variety of instabilities such as spin and charge orders, Ising superconductivity, and topological properties. Their physical properties can be controlled by doping in electric double-layer field-effect transistors (FET). However, for the case of single layer NbSe₂, FET doping is limited to $\approx 1 \times 10^{14} \text{ cm}^{-2}$, while a somewhat larger charge injection can be obtained via deposition of K atoms. Here, by performing angle-resolved photoemission spectroscopy, scanning tunneling microscopy, quasiparticle interference measurements, and first-principles calculations it is shown that a misfit compound formed by sandwiching NbSe₂ and LaSe layers behaves as a NbSe₂ single layer with a rigid doping of 0.55–0.6 electrons per Nb atom or $\approx 6 \times 10^{14} \text{ cm}^{-2}$. Due to this huge doping, the 3×3 charge density wave is replaced by a 2×2 order with very short coherence length. As a tremendous number of different misfit compounds can be obtained by sandwiching TMDs layers with rock salt or other layers, this work paves the way to the exploration of heavily doped 2D TMDs over an unprecedented wide range of doping.

1. Introduction

Transition metal dichalcogenide (TMDs) are layered materials with strong in-plane bonding and weak, van der Waals-like, coupling between the layers.^[2–12] They exhibit a rich physics with many kinds of electronic orders such as charge density wave (CDW) or superconductivity.^[1,13] In this family, single layer NbSe₂ attracted a considerable interest as it presents a CDW instability with 3×3 periodicity^[14,15] and a strong spin–orbit interaction leading to spin–momentum locking in the out-of-plane direction generating fully spin-up and spin-down polarized bands at K and K' (see **Figure 1**).^[16–18] This peculiar spin–orbit interaction has led to new developments in the field of non-conventional superconductivity, as recent measurements on monolayer and few layers NbSe₂

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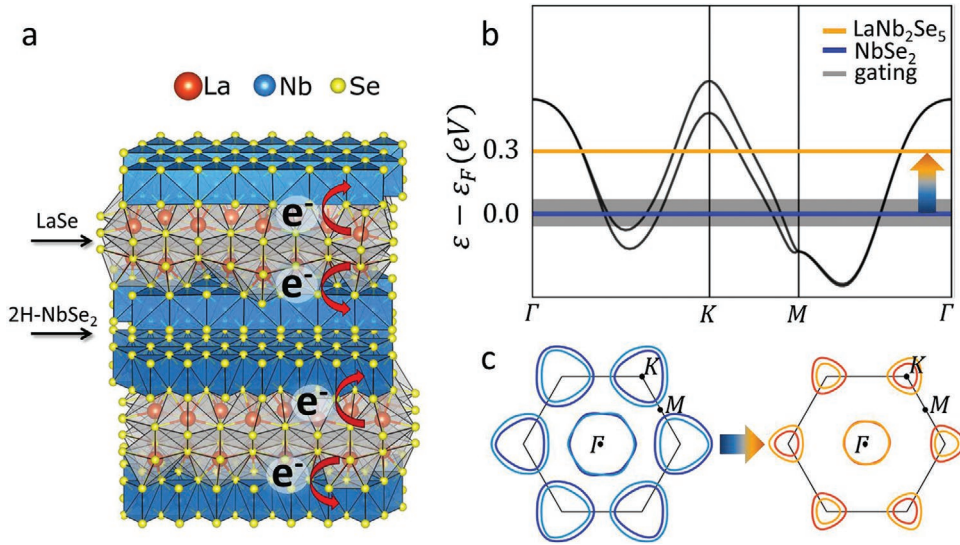


Figure 1. a) Crystal structure of $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$, the material is made of a stacking of LaSe and NbSe₂ layers. The LaSe layer is a massive electron donor. The electronic structure of $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ is very close to the one of a strongly doped NbSe₂ monolayer where energy dispersion curves around the Fermi level are illustrated by black curves in (b). The gray stripe illustrates the range of doping accessible by gating while the yellow line shows the huge doping induced by charge transfer from the LaSe layer. This huge doping results in a shrunk Fermi surface shown in (c). The Fermi surface of an undoped NbSe₂ monolayer is shown in blue, the one of $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ is shown in yellow.

samples showed that the in-plane critical magnetic field is much larger than the paramagnetic limit.^[5,19] It has been shown that both phase transitions can be partially tuned by applying a gate voltage.^[4,10] It is thus crucial to study the evolution of charge ordering and superconductivity in 2D metallic dichalcogenides in the limit of heavy electron doping, going way beyond what can be achieved by field-effect transistor (FET) doping techniques (see Figure 1).

Most of the studies on few layer NbSe₂ were done using mechanical^[20] or liquid exfoliation^[21] which implies finding a flake of sample of the appropriate thickness among the many pieces dispersed on a substrate. Doping is then achieved via FET or adatom deposition. Here, we propose an alternative technique that allowed us to investigate the extreme high-doping limit of a NbSe₂ single layer. We propose to use a compound belonging to the misfit TMDs. These misfit materials consist of TMDs layers sandwiched with rock salt chalcogenides layers,^[22] namely $(\text{RQ})_{1+x}(\text{TQ}_2)_n$ (R=Pb, Bi, or Rare-Earth, Q = Chalcogene, T = Transition metal, and $n = 1, 2$) (see Figures 1 and 2) which exhibit an intergrowth structure formed by the alternated stacking of RQ planes (having NaCl structure) with TMD layers (CdI₂ or NbS₂ structure). An electronic charge transfer occurs from the RQ to the TMD layers stabilizing the structure. It was suggested that these compounds could be considered as intercalated compounds, however it is unclear if a rigid-band model of doping could apply.^[23,24] It is possible to obtain a large variety of multilayers of TMDs (1, 2, or 3 layers) separated by insulating RQ layers. For instance, the $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ compound is composed of metallic 2H-NbSe₂ bilayers separated by insulating LaSe bilayers (Figures 1 and 2). It is even possible to use multilayers of RQ in order to get quasi-2D non-coupled NbSe₂ multilayers, thus realizing nearly ideal embedded 2D systems with a well-defined multilayer structure.

Many misfits layered compounds were found to be superconducting, like $(\text{PbS})_{1.14}\text{NbS}_2$ or $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ ^[22] with $T_c = 2.5$ K and $T_c = 5.3$ K, respectively. $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ displays an in-plane critical field around 30 T way beyond the 11.5 T paramagnetic limit required to break singlet Cooper pairs. A similar compound $(\text{LaSe})_{1.14}(\text{NbSe}_2)$, consisting of a stacking of 1H-NbSe₂ and LaSe single layers, has a critical temperature of 1.2 K and a huge in-plane critical field of more than 16 T, which is well beyond the paramagnetic limit of 2.6 T.^[25–28] This enhanced critical field is similar to what was reported for few layer NbSe₂^[5] and gated MoS₂.^[4] These unusual superconducting properties indirectly suggest that the material behaves similarly to monolayer NbSe₂ making it a bulk yet quasi-2D system. However, up to now there is no direct evidence of its bidimensionality and no measurement of the amount of doping in NbSe₂ layers.

Here we show that $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ hosts indeed a band structure that is intimately related to the one of a strongly and rigidly doped NbSe₂ monolayer. We measured finely the Fermi surface using quasiparticles interferences (QPIs) spectroscopy and angle-resolved photoemission spectroscopy (ARPES). Our measurements, supported by extensive first-principles density functional theory (DFT) calculations, demonstrate that $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ behaves as a heavily electron-doped monolayer NbSe₂ with a Fermi level shift of +0.3 eV, or equivalently ≈ 0.6 electron per niobium atom.

The general idea of our work is summarized in Figure 1b where the band structure of 1H-NbSe₂ monolayer is shown in black and the chemical potential of the undoped monolayer in blue. The gray ribbon labels the range of doping achievable with ionic liquid gating.^[29] It has to be compared with the level of doping achieved in the misfit compound via electronic charge transfer from the LaSe to the NbSe₂ layers, shown in yellow. This tremendous doping is several times larger than

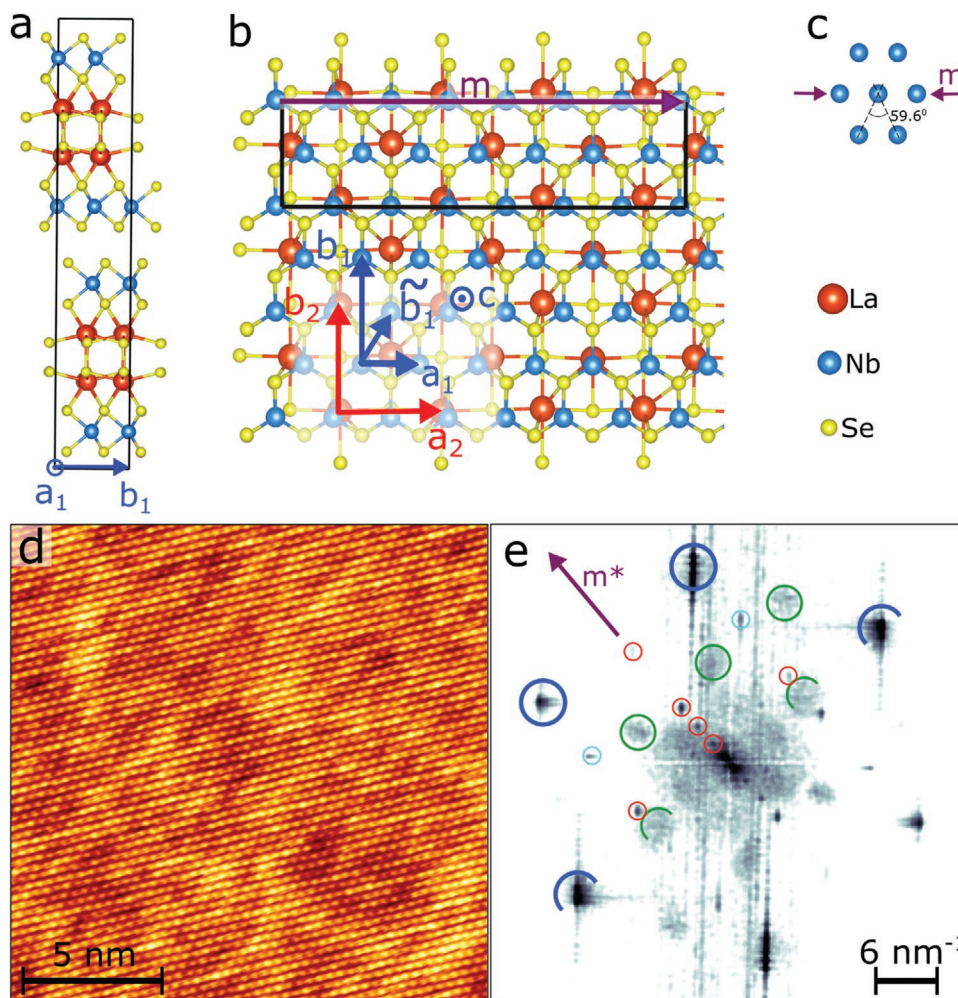


Figure 2. a) Stacking along c axis of $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$. The material can be seen like a van der Waals stacking of units composed of a LaSe layer sandwiched by two NbSe_2 monolayers. Each NbSe_2 layer is strongly bound to LaSe by ionic-covalent bonding. b) A top view is shown, the black rectangle represents a nearly commensurate approximate of the crystal structure with $m \approx 7a_1 \approx 4a_2$. The lattice of the NbSe_2 layers is not perfectly hexagonal, it is slightly compressed along the b_1 direction as shown in (c). In (d), STM topography of a cleaved $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ sample measured at 4.2 K ($V_T = -200$ mV). The triangular atomic lattice indicates that the sample is terminated by a NbSe_2 layer. e) Fourier transform modulus of the topography. The dark blue circles indicate the NbSe_2 Bragg peaks and the red circles highlight some incommensurability peaks due to the modulation of the NbSe_2 lattice by the underlying LaSe lattice. The light blue circles correspond to the underlying LaSe lattice. The green circles are associated to a 2×2 charge modulation with a short coherence length.

what can be achieved by conventional ionic liquid doping in FET geometry. As a consequence, the shape of the Fermi surface is greatly modified and in particular the Fermi pockets at Γ and K are strongly shrunk as our QPIs and ARPES measurements reveal. The ability to induce a huge doping such as to change dramatically the shape of the Fermi surface is extremely promising for future work on electronic properties of misfit compounds.

2. Structure

The misfit material $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ is a layered compound consisting of a regular alternation of 2H- NbSe_2 bilayers with trigonal prismatic structure and of rocksalt two atom thick LaSe layers (Figures 1 and 2). Each NbSe_2 and LaSe sublattice has its own set of cell parameters noted a_ν , b_ν , and c_ν , with $\nu = 1$ and

2, respectively. Compared to bulk 2H- NbSe_2 the lattice of NbSe_2 layers is not perfectly hexagonal and is slightly compressed along the \bar{a}_1 direction (space group C_{2221} , see Figure 2c). As a consequence, the NbSe_2 sublattice is described by a centered orthorhombic cell with in-plane lattice vectors $a_1 = 3.437$ Å and $b_1 \approx 6$ Å. The LaSe sublattice has also an orthorhombic symmetry but with similar in-plane lattice parameters $a_2 \approx b_2 \approx 6$ Å. Both NbSe_2 and LaSe layers have the same \bar{b} lattice vector ($\bar{b}_1 = \bar{b}_2$) and the material is commensurate in this direction. However, the ratio between the norms of the \bar{a}_1 and \bar{a}_2 vectors, sharing a common direction, is an irrational number ($a_2/a_1 = 1.751 \approx 7/4$), making $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ incommensurate in the \bar{a} direction. However, $a_2/a_1 \approx 7/4$ such that $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ can be considered as almost periodic in the \bar{a}_2 direction with an approximate commensurate lattice vector \bar{m} ($m = 7a_1 \approx 4a_2$).

A commensurate structure with $m = 7a_1 \approx 4a_2$ was assumed in first-principles electronic structure calculations (see the

Experimental Section). We performed structural optimization for the full bulk structure (232 atoms per cell). We used different starting guesses obtained by superimposing in different ways LaSe and NbSe₂ bilayers (see Supporting Information). Minimization of the total energy gives two inequivalent minima that however result in very similar structures with practically identical electronic structures. Very strong ionic-covalent bonds form at the contact between NbSe₂ and LaSe with a substantial deformation of the LaSe layer (see Figure 2 and movie in Supporting Information) and a significant deviation from an ideal rock salt structure. This huge modification of the LaSe interface signals a large charge transfer between LaSe and NbSe₂ bilayers. On the contrary the van der Waals interface between the two NbSe₂ layers is weakly affected. This explains why the cleavage of the sample leads to a monolayer (ML) NbSe₂ terminated surface (see Figures 1 and 2) that we probed by scanning tunneling microscopy (STM) and ARPES.

A typical STM topography map of (LaSe)_{1.14}(NbSe₂)₂ surface of an in situ cleaved sample is represented in Figure 2d. Since the surface layer is 1H-NbSe₂, the atomically resolved STM images show the Se atoms of NbSe₂. The rectangular centered Se lattice appears almost hexagonal and for simplicity, in the following, the NbSe₂ layers will be referred as hexagonal. In addition to the Se atomic lattice, one observes multiple additional spatial modulations which are due to the incommensurability with the underlying LaSe layer. In order to properly characterize the origin of these modulations, the modulus of the Fourier transform of a similar but larger scale topographic image taken on the same area with same scanning angle is represented in Figure 2e. The Bragg peaks of the reciprocal lattice of NbSe₂ are highlighted by blue circles. The sharp peaks circled in red are the first, second, third and sixth harmonics of the approximate periodic misfit potential. Additional peaks attributed to the LaSe lattice are also observed and accented by light blue circles. The signals presented so far can directly be deduced from the theoretical crystalline structure. In addition to those, one can also observe other contributions. First, diffuse peaks (highlighted by green circles) lie at half the Bragg peaks of the NbSe₂ hexagonal lattice. They express the presence of a 2 × 2 charge modulation in the system. This charge order will be fully discussed later in this paper. In addition, a halo surrounding Γ quasi-reaching half the Bragg peaks can be seen. It is attributed to integrated QPI spectroscopic signal as we discuss below.

3. Electronic Band Structure

We then study the electronic structure of the surface of NbSe₂ terminated (LaSe)_{1.14}(NbSe₂)₂ by using DFT calculations. The results are presented in Figure 3e after band unfolding^[30,31] onto the NbSe₂ three-atom C₂₂₂₁ pseudo-hexagonal unit cell having $a_1 = 3.457$ Å and $\tilde{b}_1 = 3.437$ Å ($\tilde{b}_1 = (a_1 + b_1)/2$, see Figure 2b). As a reference, we also plot in red the electronic structure of an isolated 1H-NbSe₂ layer with the same a_1 and \tilde{b}_1 but doped by 0.6 electrons per Nb atom (we use a compensating positive background to ensure charge neutrality). As can be seen, the electronic structure of (LaSe)_{1.14}(NbSe₂)₂ in a ± 0.5 eV range from the Fermi level is almost indistinguishable

from that of a rigidly doped NbSe₂ monolayer. This is further confirmed by the detailed comparison of the electronic structure of the (LaSe)_{1.14}(NbSe₂)₂ surface with that of a rigidly doped single layer NbSe₂ with C222₁ unit cell (see Figures S1 and S2 in Supporting Information). The only differences occur at zone center where a lanthanum band hybridizes with the single layer NbSe₂ band. The resulting band deformation leads to a small La component at the Fermi level (ϵ_F) close to zone center. The amount of La electrons at ϵ_F remains, however, negligible, as demonstrated by the density of states projected over La and Nb atomic states in the rightmost panel of Figure 3e. Finally, we underline that, even if we keep in all simulations, the non-perfect hexagonal symmetry due to the anisotropy in a_1 and \tilde{b}_1 , this effect is completely irrelevant and does not lead to any sizeable effect in the electronic structure and Fermi surface. The calculated Fermi surface of the isolated layer is plotted in Figure 3d with the degree of spin up and down polarization illustrated in different colors.

We probed the band structure at Fermi energy by QPI spectroscopy measurements on NbSe₂ terminated (LaSe)_{1.14}(NbSe₂)₂. This technique relies on the scattering of the electron Bloch functions by defects. The incoming and scattered electrons may give rise to some interference pattern that can be measured by scanning tunneling spectroscopy. In Figure 2e some QPIs are already appearing, but they are not well resolved. This is due to the fact that the topography was recorded with a bias of 200 mV and, as such, it is sensitive to the integral of the local density of states in an energy window of 200 meV. Thus the spectroscopic halo around Γ in Figure 2e is actually a mix between the QPIs patterns at all energies ranging from 0 to -200 meV. In order to get a highly resolved QPIs measurement of the band structure at the Fermi energy we performed topography measurements with a low voltage of 20 mV so that only electrons in a 20 meV window close to ϵ_F contributed (Figure 3a). As the band dispersion over a 20 meV range is negligible (see Figure 3e), these measurements should reflect the joined density of states at the Fermi level (see Experimental Section). The Figure 3a shows a Fourier transform of the topography which spans many Brillouin zones. One can observe a dark vertical band which indicates that a stronger QPI signal is generated in the direction of the incommensurability. This suggests that the incommensurability plays the role of electron scattering potential. Moreover, as atomically resolved images in Figure 2 do not present any visible defects such as vacancies, steps, or dislocations (i.e. the samples are very clean), the only scattering mechanism susceptible to generate QPIs is provided by the incommensurability.

In order to get more insight on the band structure we performed QPIs measurements by taking the squared modulus of Fourier transform of conductance maps measured at the Fermi energy. Such a QPIs measurement is shown in Figure 3b, where one can see a complex structure with some almost circular patterns. The different circular patterns are associated to different scattering mechanisms shown in Figure 3d. For instance the Q_1 vector depicts scattering events from the Γ pocket to itself, while Q_2 depicts scattering between the Γ pocket and the outer K or K' pockets. Finally, the vector Q_3 schematizes scattering in between Γ and the internal K and K' pockets. These different scattering channels lead to the nearly circular patterns depicted

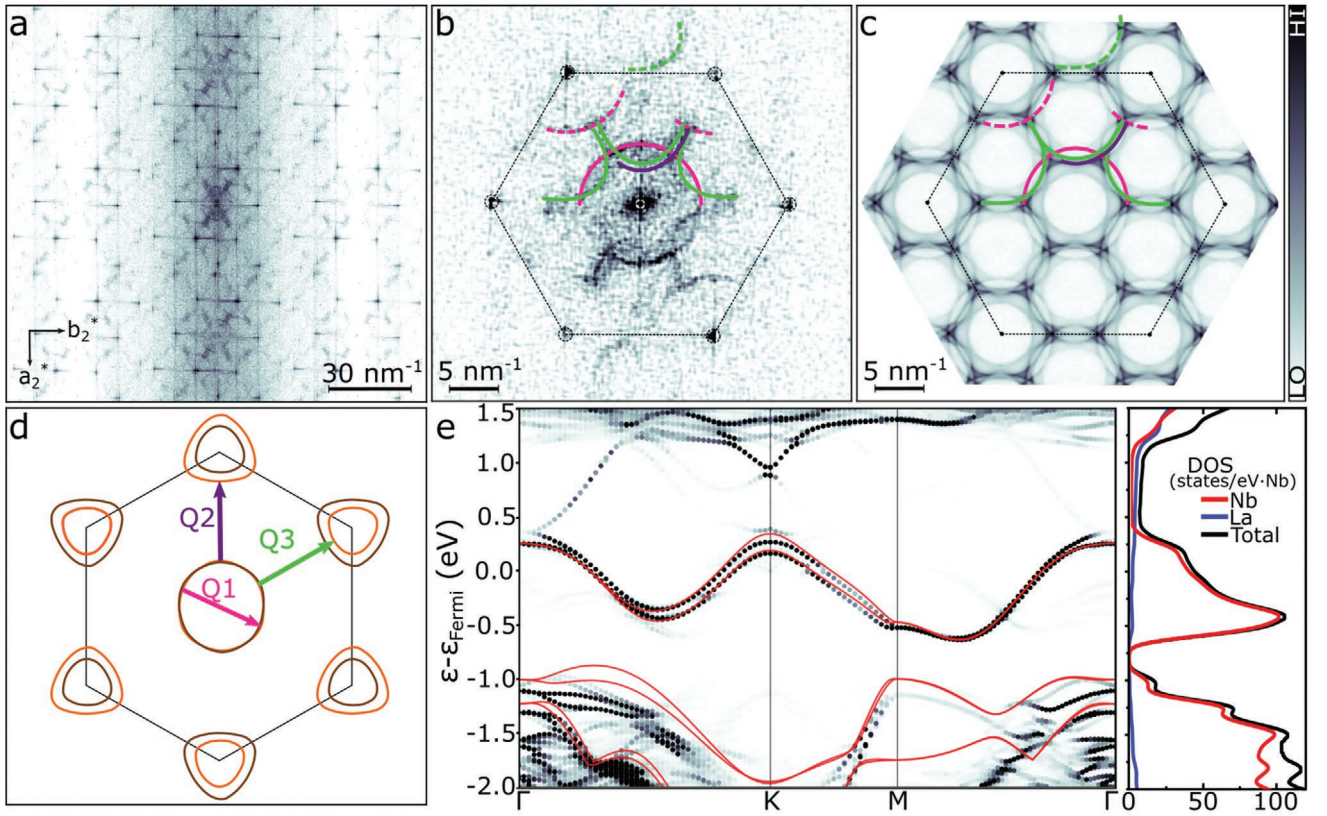


Figure 3. a) Fourier transform modulus of a highly resolved STM topography of $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ ($T = 4$, 2 K, $V_T = -20$ mV) showing QPIs over several NbSe₂ Brillouin zones. The signal in dark gray is stronger in the b_1^* direction which corresponds to the direction of the incommensurability. b) Fourier transform of a conductance map at Fermi energy ($T = 4$, 2 K). A DFT simulation of the QPIs is shown in (c), with the same highlighted details as in (b). d) Fermi Surface of a 1H-NbSe₂ monolayer for the doping level found in $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$. The different color of the Fermi surface at K and K' corresponds to the different out-of-plane spin polarization. A few scattering channels implied in the QPI images are shown with arrows. e) The unfolded electronic band structure of $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ is shown in gray dots, the dot color scale following the spectral weight of the band. It is compared with the dispersion of a NbSe₂ monolayer (red curve). The right panel of (e) displays the contribution from La and Nb atoms to the density of states.

in color on Figure 3b. We calculated the QPI patterns (see Experimental Section and Supporting Information) by using DFT for a three atom NbSe₂ unit cell for an unsupported monolayer with a doping of ≈ 0.55 – 0.6 electrons per Nb atom. The simulated QPI, shown in Figure 3c, exhibits the same circular patterns as the experiment. In order to compare quantitatively the experimental and theoretical QPIs, we plotted an identical set of circles on both Figure 3b,c, where the color corresponds to different scattering channels as explained above. The agreement is very good; all the patterns observed experimentally are accurately reproduced by the rigid-band approximation of 1H-NbSe₂ monolayer doped by ≈ 0.55 – 0.6 electrons per Nb, except some spectral weight at the Bragg peaks. This latter electron doping agrees well with the chemical estimate that, in $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$, the $(\text{LaSe})_{1.14}$ should provide 1.14 electrons to $(\text{NbSe}_2)_2$. This simple chemical intuition leads to 0.57 electron doping which is in very good agreement with DFT and experiments.

One of the major interests of single layers 1H TMDs is their Ising spin–orbit splitting. This spin–orbit splitting should manifest with two scattering channels corresponding to the scattering from Γ to the outer K pocket and from Γ to the inner K pocket, represented schematically by Q_2 and Q_3 , respectively, in

Figure 3d. This should lead to two concentric circles schematized by the purple and green arcs in Figure 3b,c. This splitting is indeed observed even though the signal-to-noise ratio is pretty weak.

According to our QPIs measurements and DFT calculations we found that the band structure of the NbSe₂ terminated surface of $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ is well accounted for by a rigid-band approximation with a huge Fermi level shift. In order to ascertain this finding, we carried out some comparative ARPES measurements of the low-energy electronic states of bulk 2H-NbSe₂, K-doped 2H-NbSe₂ (see Experimental Section) and $(\text{LaSe})_{1.14}(\text{NbSe}_2)_2$ at $T = 50$ K and using He-I radiation ($h\nu = 21.2$ eV). Figure 4a,b shows the corresponding ARPES intensity maps along the $\bar{K}'\text{--}\bar{M}\text{--}\bar{K}$ and $\bar{K}'\text{--}\bar{\Gamma}\text{--}\bar{K}$ high-symmetry lines of the hexagonal surface Brillouin zone of 2H-NbSe₂ (Figure 4c), respectively. Around \bar{M} , for pristine 2H-NbSe₂ (Figure 4, left panel), we can easily recognize the spin-polarized Nb *4d*-derived states coming from the cut of the two strongly trigonally warped barrels of the Fermi surface centred around each zone-corner \bar{K} (\bar{K}') point (also see the calculated Fermi surfaces in Figure 3).^[18] At $\bar{\Gamma}$ (Figure 4b, left panel), whereas the Nb-dominated states yield strong spectral weight close to the Fermi level crossings away from normal

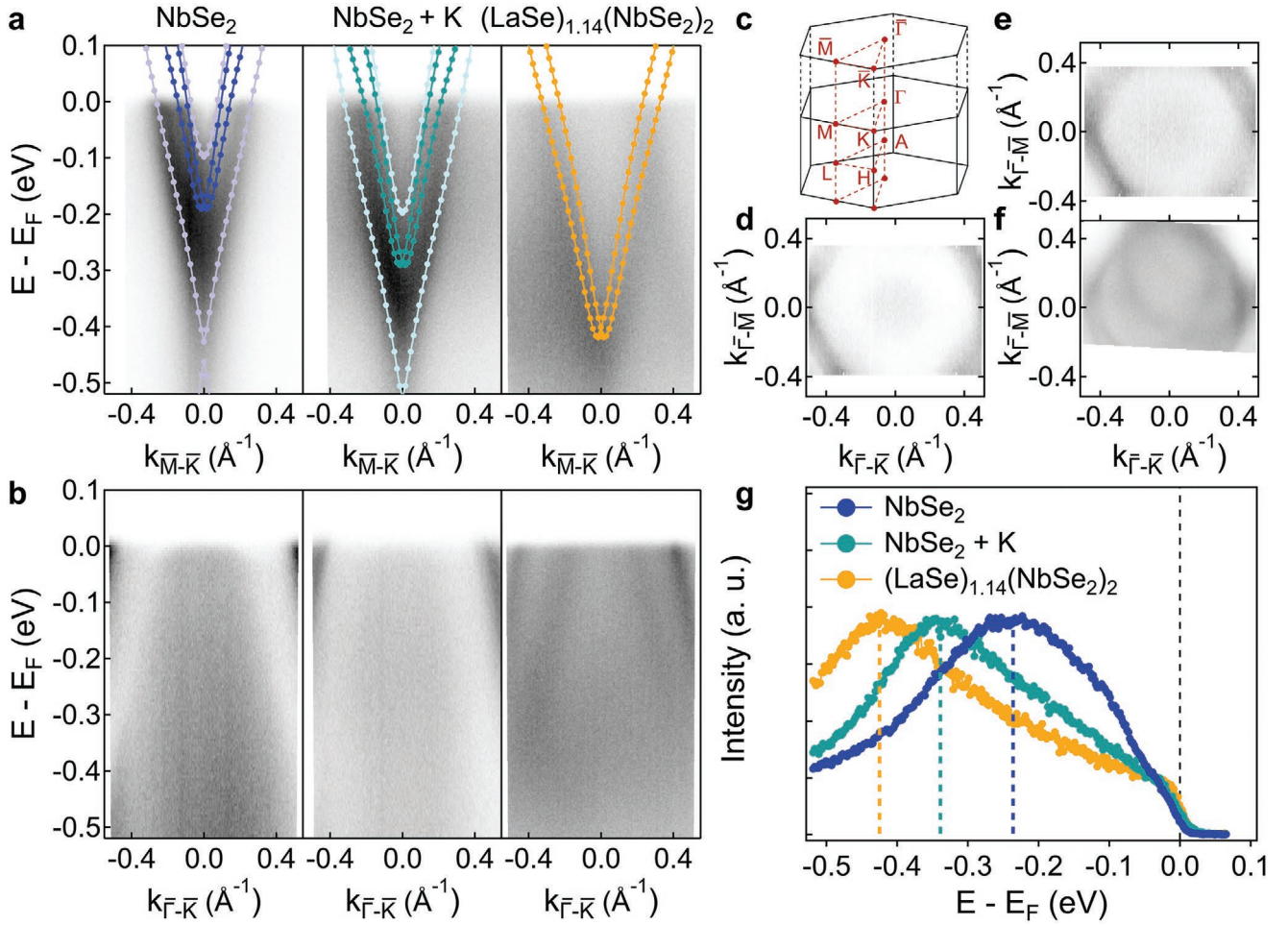


Figure 4. a) From left to right: ARPES spectra along the $\bar{K}'-\bar{M}-\bar{K}$ high-symmetry line of the Brillouin zone of pristine NbSe₂ (left), K-doped NbSe₂ (middle) and of the misfit compound (LaSe)_{1.14}(NbSe₂)₂, measured using HeI photon energy ($h\nu=21.2$ eV) and at $T = 50$ K. On the left panel the pristine NbSe₂ band structure calculated by DFT is shown in light blue for $k_z = 0$ and dark blue for $k_z = 1/2$. In the middle panel the same DFT curves are shown shifted by 0.1 eV. In the right panel, the orange dotted curve represents the DFT calculated band structure of a monolayer NbSe₂ with a doping of 0.55–0.6 electrons per Nb atom. b) Same as (a) along the $\bar{K}'-\bar{\Gamma}-\bar{K}$ high-symmetry line of the Brillouin zone. c) Surface and 3D Brillouin zone of 2H-NbSe₂. Fermi surfaces around the $\bar{\Gamma}$ point of the Brillouin zone of d) pristine NbSe₂, e) K-doped NbSe₂, and of f) the misfit compound (LaSe)_{1.14}(NbSe₂)₂. g) Energy distribution curves taken at \bar{M} on a) for pristine NbSe₂ (blue), K-doped NbSe₂ (green) and of the misfit compound (LaSe)_{1.14}(NbSe₂)₂ (orange). The coloured vertical dashed lines indicate the energy position of the maxima of the EDCs corresponding to the bottom of the electron pockets at \bar{M} associated with the three different samples.

emission, additional diffuse spectral weight coming from a highly 3D Fermi surface sheet of predominantly Se p_z orbital character is visible at the zone centre due to the finite out-of-plane momentum resolution of ARPES (also see the measured Fermi surface Figure 4d).^[18]

The same spectral features are also seen for the K-saturated surface of NbSe₂ with a yet higher diffuse background (coming from the randomly adsorbed alkali atoms at the NbSe₂ surface) and a different chemical potential as evidenced by the shift toward higher binding energies of both the electron pocket at \bar{M} and the hole pocket at $\bar{\Gamma}$ (Figure 4a,b, middle panels) and the reduced area of the $\bar{\Gamma}$ -centered Fermi surface (Figure 4e). As at the photon energy used here, the inelastic mean free path of the photoelectrons is on the order of the interlayer distances, we are predominantly sensitive to the doping of the topmost layer of the unit cell. From our ARPES measurements, we can

thus conclude that the K-saturated NbSe₂ surface has been electron doped within a rigid-band picture corresponding to a chemical potential shift of ≈ 100 meV.

Focusing now on (LaSe)_{1.14}(NbSe₂)₂, we observe further energy shifts toward higher binding energy of both the electron and hole Nb-derived pockets (Figure 4a,b, right panels) as well as a still reduced Fermi surface area (Figure 4f). This indicates that the electron doping of the NbSe₂ layer at the interface with LaSe within the misfit compound is much higher than the one obtained by alkali gating. Energy distribution curves taken at the \bar{M} point for bulk NbSe₂, K-doped NbSe₂ and (LaSe)_{1.14}(NbSe₂)₂ (Figure 4g) demonstrate that such a doping is almost twice the one reached in K-doped NbSe₂ with a chemical potential shift of ≈ 190 meV (see the vertical dashed lines on Figure 4g showing the energy position of the bottom of the electron pockets at \bar{M}) with respect to pristine NbSe₂. Interestingly, we can also note the

absence of spectral intensity coming from the Se p_z orbital at the zone centre (Figure 4b, right panel), indicating that the band structure of NbSe₂ within the misfit compound is close to the one of a strongly electron-doped NbSe₂ *monolayer*. Nevertheless, the electrons feel a rather strong competing potential coming from the intrinsic incommensurability of the heterostructure as evidenced by the clear presence of shadow bands not only in the ARPES intensity maps but also at the Fermi surface (Figure 4f).

4. Emergence of 2×2 Charge Ordering

Bulk 2H-NbSe₂ shows a CDW transition at around 35 K with a nearly commensurate 3×3 charge order.^[2] In single layer, contradictory results have been reported as ML NbSe₂ on top of Graphene shows a strong increase of T_{CDW} with respect to the bulk,^[14] while ML NbSe₂ grown on top of SiO₂ shows a 3×3 CDW with a similar T_{CDW} as in the bulk. Recent first-principles calculations^[32] confirm the second behavior. It has been shown that electron doping by FET strengthens T_{CDW} ,^[10] it is however unclear if a change of ordering vector occurs. The continuous T_{CDW} curve versus FET doping in ref. [10] seems to suggest that it is not the case, however the range of considered doping is much lower.

Since (LaSe)_{1.14}(NbSe₂)₂ shows an energy band structure analogous to 1H-NbSe₂ monolayer one expects CDW to show up at low temperatures. It is well established that CDW are in general very sensitive to the shape of the Fermi surface. Thus, one expects that the strong doping of 0.55–0.6 electrons/Nb could induce some change in the CDW periodicity. This is indeed the case as we found no experimental evidence of a 3×3 charge ordering, but we find 2×2 patches appearing below ≈ 105 K in most parts of the sample. Our experimental observations are summarized in **Figure 5**, where a topography with a 2×2 charge order is shown in panel (a), while the Fourier transform modulus of the topographies measured at various temperature are shown in (b). The Fourier transform shows a sixfold peak structure at half-Bragg positions that corresponds to a 2×2 charge modulation in real space. The 2×2

signal is still present in Fourier map at 100 K and it disappears above 105 K (see Figure 5b). However, the 2×2 reconstruction does not cover completely the sample in a uniform way, but is more clearly visible in some regions with respect to others. The corresponding CDW peak in Figure 5 is also less sharp, probably meaning that regions of 2×2 ordering coexist with patches with no CDW ordering.

In order to investigate the possible evolution of T_{CDW} with doping, we performed harmonic phonon calculations using density functional perturbation theory^[33,34] for a single layer NbSe₂ as a function of electron doping. The system is kept neutral by using a positive jellium background. The hexagonal compression of the lattice is included, so that there are two inequivalent M points (labeled M and M'). The results are shown in Figure S3, Supporting Information. At zero doping, we find a broad region of instability close to $2/3\Gamma M$ and $2/3\Gamma M'$, compatible with a 3×3 CDW, signaled by the occurrence of an imaginary mode both along ΓM and $\Gamma M'$. At a doping of 0.4 electrons/Nb, the region of instability shifts at the M and M' points, in qualitative agreement with experimental findings. It is known that^[32] the CDW in NbSe₂ arises from an interplay between Fermi surface effects and ionic fluctuations related to anharmonicity. Fermi surface effects determine the ordering vector, while the occurrence of the CDW is mostly related to phonon–phonon scattering. In our calculation we only include harmonic terms, thus we overestimate the tendency toward CDW. At a doping of 0.4 electrons/Nb, the ordering vector changes essentially because the Fermi surface geometry is affected and a nesting compatible to 2×2 reconstruction occurs. However, at the doping of 0.55–0.6 electrons/Nb, that is the one estimated by comparing our electronic structure with QPI and ARPES, no instability is found, mainly because the vector $q = 0.5$ does not connect efficiently the portion of the Fermi surface. Anharmonicity would suppress even more the CDW instability. A possible way to reconcile theory and experiments, is to consider a non-uniform doping in the sample and the possible existence of patches with lower doping. These regions are not detected in ARPES and QPI that probe larger regions of the sample, however they can be detected by the ultrafine spatial sensitivity of STM.

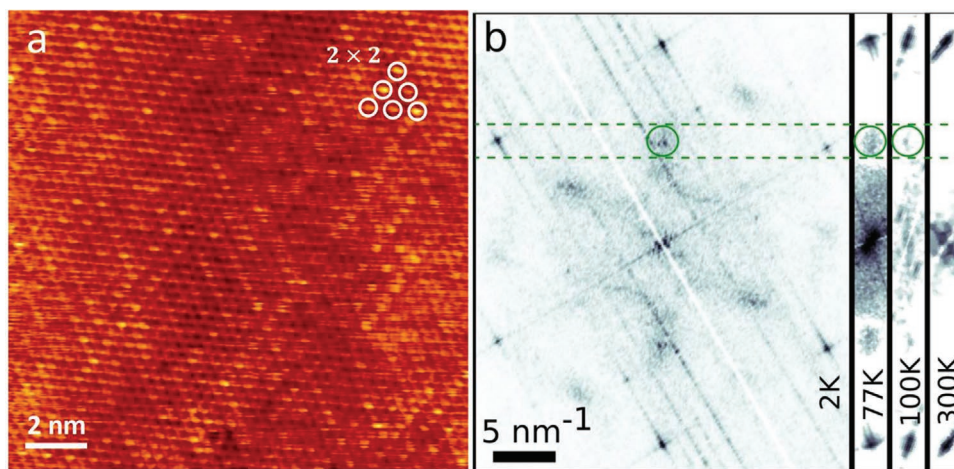


Figure 5. a) STM topography evidencing 2×2 charge modulation with a short coherence length ($T = 2$ K, $V_T = 24$ mV). b) The corresponding Fourier transform modulus. The right panel in (b) shows the evolution of the Fourier transform modulus with temperature. The 2×2 pattern is still visible at 100 K, it disappears at ≈ 105 K.

5. Conclusion

The success of 2D crystals in the fields of physics, nanotechnology, chemistry, and material science is largely due to the much greater tunability of their properties with respect to their bulk counterparts. The three main parameters that can be varied are the sample thickness, the Moiré angle between the stacked layers, and doping. However, while the first two parameters can be varied at will, for NbSe₂ doping is limited to $\approx 10^{14}$ electrons cm⁻²,^[29] that is the maximum amount of carriers that can be introduced in an electrical double-layer FET geometry. Somewhat larger doping can be achieved via deposition of alkali atoms (such as potassium). However, in many cases, the deposition of alkali atoms on a 2D crystal is difficult to achieve as the coverage can be non-uniform or the wetting of the 2D crystal by the adatoms not even possible.

Here we propose to use rocksalt rare-earth chalcogenides sandwiched with TMDs to build a misfit compound. Both the thickness of the TMD and of the rocksalt rare-earth chalcogenide can be tuned at will,^[11,12] exactly as in a 2D crystal. The large electron charge transfer from the rare-earth chalcogenide to the TMD allows to obtain doping fractions that largely encompass both those obtained in the case of ionic-liquid-based FETs and K adatom deposition. We have shown that this is indeed the case for NbSe₂ bilayers sandwiched in rocksalt LaSe for which we achieve a doping of 0.55–0.6 electrons per Nb, corresponding to a ≈ 0.3 eV shift of the Fermi level. This large electron transfer from LaSe to the TMD is due to the chemical properties of the highest occupied states of bulk LaSe that are formed only by atomic La states.^[35] As a consequence LaSe essentially behaves as a donor, an effect that we expect not to depend on the kind of TMD used to build the misfit structure. This suggests that similarly large doping can be achieved by sandwiching LaSe with other metallic TMDs.

Finally, we remark that it is also possible to vary the rock-salt layer, opening a tremendous space of possibilities and a fertile ground for the discovery of highly innovative materials. For instance, assuming La³⁺, Pb²⁺, and Se²⁻ in the hypothetical series of compounds (La_{1-y}Pb_ySe)_{1+x}(NbSe₂)₂, a simple charge balance calculation shows that the charge transfer from the rock salt layer (La_{1-y}Pb_ySe) to the (NbSe₂)₂ double layer could vary continuously from 0 to 1 + x by reducing the lead content. While the (La_{1-y}Pb_ySe)_{1+x}(NbSe₂)₂ series was never reported so far, similar substitutions of La³⁺ per Sr²⁺ substitution were already demonstrated in the (LaS)_{1+x}VS₂^[36] and (LaS)_{1+x}CrS₂.^[23] Therefore, the charge transfer could be tuned by appropriate substitution in misfit layer compounds, pretty much in the same way as doping can be varied in FET, but in a much broader range.

We have shown that the effect of a large electron doping in single layer NbSe₂ results in the change of the ordering vector of the CDW. However, other properties can also be explored in misfit compounds, such as topological and Ising superconductivities in NbSe₂ and MoS₂, Mottronics with misfit compounds involving 1T-TaSe₂ or 1T-NbSe₂ layers^[37–39] or thermoelectric applications^[40–42] where the ability to fine tune the chemical potential in stacks of 2D topological insulators such as 1T'-WSe₂ would be a perfect tool for rational design of materials with high figures of merit.

6. Experimental Section

Single crystals of (LaSe)_{1.14}(NbSe₂)₂ were prepared by the solid-state reaction of the elemental precursors (i.e., La, Nb, Se) and subsequent chemical vapor transport using I₂. Under inert atmosphere, millimeter-sized La powder was freshly scraped from the ingot (Strem Chemicals, 99.9%) and mixed with Se (Alfa Aesar, 99.999%) and Nb powder (Puratronic, 99.99%) in the molar ratio of La/Nb/Se = 1.14/2/5.40. Here Se was added in 5% excess over the nominal stoichiometry La/Nb/Se = 1.14/2/5.14. The mixture was manually ground in an agate mortar and transferred in a silica tube (15 cm), which was subsequently evacuated to 10⁻³ torr and sealed by flame. The sealed mixture was firstly heated to 200°C at a rate of 50 °C h⁻¹ and held for 12 h. Then the temperature was raised to 900 °C at the same rate and heated for 240 h before the furnace was subject to radiative cooling. The lustrous black powder (ca., 500 mg) obtained from the reaction was placed in the clean silica tube (length: 15 cm) together with 43 mg of iodine (Aldrich, 99.9%), followed by the evacuation at liquid nitrogen temperature (77 K) and flame sealing. The reaction mixture was loaded into the furnace designed to create temperature gradient: the lump of the mixture was heated at 900 °C on one side of the tube and the other side was held around 750 °C. After 240 h of the thermal treatment, the reaction was quenched by plunging the tube into water. The single crystals grown on the wall of tube were washed with water and ethanol and stored in vacuum. The compositional integrity of the obtained crystals was checked by their backscattered electron images and energy-dispersive X-ray (EDX) spectra acquired on scanning electron microscopy (JEOL JSM 5800LV).

In order to access the LDOS at different energies, spectroscopic *I*(*V*) maps were acquired, consisting in taking individual *I*(*V*) spectra at many positions determined by a predefined spatial grid. The differential conductance *dI/dV* maps (derived afterward) at a given voltage *V* can directly be related to the LDOS of the sample at the corresponding energy. Performing LDOS experiments at 4.2 K allowed us to exhibit QPIs patterns which give access to the Fermi surface of (LaSe)_{1.14}(NbSe₂)₂. The study was realized with an Omicron LT STM and a home-made 300 mK STM using Pt80%/Ir20% tips. Prior to each experiment, the DOS of the tip was verified on Pt and HOPG samples and checked to be featureless. The topography maps were taken in constant current mode and the spectra were taken at constant tip-sample distance for a given tunneling set point (mainly around *U* = -20 mV, *I* = 100 pA). The samples were cleaved at room temperature in ultrahigh vacuum under a pressure of $\approx 5 \cdot 10^{-11}$ mbar directly before being loaded into the STM head.

Clean NbSe₂ surfaces were obtained by cleaving NbSe₂ single crystal and (LaSe)_{1.14}(NbSe₂)₂ in ultrahigh vacuum at room temperature. The K-doped surface has been obtained by evaporating K atoms in situ from a carefully outgassed SAES getter source onto the NbSe₂ surface kept at ≈ 50 K to inhibit K intercalation. During the K evaporation, the pressure was maintained below 5×10^{-10} mBar. The ARPES measurements were carried out using a Scienta DA30 photoelectron analyser with He-I radiation (*hν* = 21.22 eV). The total energy resolution was 5 meV and the base pressure during experiments was better than 1.5×10^{-10} mbar.

DFT calculations were performed by using the QUANTUM-ESPRESSO (QE) package.^[33,34] The generalized gradient approximation in the PBE parameterization^[43] for the exchange–correlation functional was adopted. The kinetic energy cutoff for plane-wave expansion had been set to 45 Ry (537 Ry for the charge density). In the case of non-collinear spin–orbit coupling (SOC) calculation, ultra-soft fully relativistic pseudopotential, directly downloaded from the QE repository was used.^[44] In this case an energy cutoff of 75 Ry (537 Ry for the charge density) was used. Integration over the Brillouin Zone (BZ) was performed using an uniform $4 \times 1 \times 1$ Monkhorst and Pack^[45] grid. For all of the calculations a Gaussian smearing of 0.01 Ry was adopted. For more details see Supporting Information.

The structural optimization for the bulk had been carried out by using as starting guess the experimental work of Roesky et al.^[46] A $\sqrt{3} \times \sqrt{3}$

NbSe₂ bilayer supercell of the compressed hexagonal unit cell was built and piled it up to a 1×4 supercell of the LaSe bilayer (see Supporting Information for more details). Similar calculations had been carried out for the NbSe₂ terminated surface.

QPI spectra had been calculated adopting the Green function formalism, by using the following expression $\rho(\mathbf{q}, \omega) = -\frac{1}{\pi N_k} \text{Im} \sum_{nk, m} M_{nk, mk+q} G_{nk}^0(\omega) G_{mk+q}^0(\omega)$, where $G_{nk}^0(\omega) = 1/(\epsilon_{kn} - \omega - i\eta)$ is the Green function obtained from the relativistic band structure ϵ_{kn} and $M_{nk, mk'}$ is the matrix element due to scalar impurities that guarantees the spin conservation in the scattering process. As QPI spectra required ultradense k-point grids, the Wannier90 code^[47–49] was used and the integration was performed over a uniform 120×120 k-point grid.

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Author Contributions

S.S. and L.C. grew the crystals and analyzed them by X-ray diffraction and X-ray spectroscopy. R.T.L., A.P.-M., C.B., I.A., O.S., T.S., and T.C. contributed to STM/STS and transport experiments. F.D. and P.D. supplied technical support for the STM setups. T.J., C.M., and G.K. performed the ARPES experiments. M.C., C.T., and M.C. performed the DFT calculations.

Data Availability

The datasets generated and analyzed during the current study are available from the corresponding author (T. C.) upon reasonable request.

Keywords

charge density waves, highly doped materials, misfit compounds, single layer materials, transition metal dichalcogenides

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