

# Field-induced polaron formation in the Holstein-Hubbard model

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**Abstract** – We study the effect of strong DC and pulsed electric fields on a Mott insulating system with coupling to optical phonons. A DC field of the order of the gap induces a metallic state characterized by polaronic features in the gap region and a partially inverted population. In this quasi-steady state, the field-induced doublon-hole production is balanced by a phonon-enhanced doublon-hole recombination. The photo-excitation of carriers by a pulsed field leads to similar modifications of the electronic structure in the gap region, and an associated reduction of the doublon life-time. We demonstrate that the field-induced localization of electrons effectively enhances the phonon coupling, an effect which should be measureable with time-resolved photo-emission spectroscopy.

Strong electric fields and other external perturbations can entirely change the properties of correlated electron materials. If a small DC electric field is applied to a Mott insulator, it merely induces a polarization, but if the field exceeds a certain threshold, carriers can tunnel across the gap [1–4], which leads to a nonequilibrium metallic state. For an isolated system, the field-induced carriers quickly heat up to infinite temperature and the current vanishes [5–8], but with dissipation, a nonequilibrium steady state with a nonthermal energy distribution may be established. Alternatively, mobile charge carriers can be introduced into a Mott insulator by a laser pulse whose frequency is tuned to the Mott gap [9–11]. Here an efficient dissipation mechanism may cool photo-excited hot carriers before they recombine, and thus lead to a photo-doped metallic state which is different from a chemically doped metal [12].

In real materials, the lattice acts as a heat bath for the electrons. In a metal, the energy transfer from the electrons to the lattice is often described by weak-coupling theory [13], or by the phenomenological two-temperature model [14], which relies on the assumption that the electron dynamics is fast compared to the phonons. However, in strongly interacting systems, this separation of timescales is in general not possible. For example, the strongly coupled molecular vibrations in organic Mott insulators have frequencies comparable or even larger than the electronic bandwidth [15–18], and conversely, the relaxation times of charge excitations in Mott insulators

can become much longer than the fast electronic hopping times [10,17,19,20]. In a theoretical description of a dielectric breakdown or photo-doping process, it can thus be important to treat the electronic system and the lattice on equal footing. For a single electron coupled to the lattice, calculations based on exact diagonalization for the Holstein model predict intriguing nonlinear transport phenomena [21], and a relaxation of photo-excited carriers on the timescale of the hopping [22]. In interacting electron systems, *e.g.* the half-filled Mott insulator, exact diagonalization [23,24] and density-matrix renormalization group [25] calculations for the Holstein-Hubbard and Holstein- $tJ$  models have been used to study the relaxation dynamics of photo-carriers. For higher excitation densities, the situation is however unclear.

In this work we consider the Holstein-Hubbard model in the Mott insulating phase and drive it out of equilibrium by applying strong electric fields. The model describes electrons with local interactions and a coupling to dispersionless phonons,

$$H(t) = - \sum_{i,\delta,\sigma} v_{i,i+\delta}(t) c_{i+\delta,\sigma}^\dagger c_{i,\sigma} + \sum_i [\omega_0 b_i^\dagger b_i + U n_{i,\uparrow} n_{i,\downarrow}] + \sum_i [-\mu(n_{i,\uparrow} + n_{i,\downarrow}) + g(n_{i,\uparrow} + n_{i,\downarrow} - 1)(b_i^\dagger + b_i)]. \quad (1)$$

Here,  $U$  is the on-site repulsion,  $\mu$  the chemical potential of the electrons with creation operators  $c_\sigma^\dagger$  and density operators  $n_\sigma$ ,  $b^\dagger$  the creation operator for Einstein

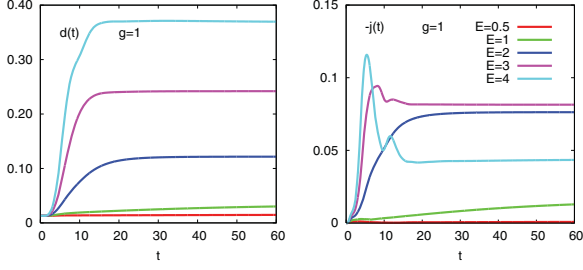


Fig. 1: (Colour on-line) Time-evolution of the double occupancy  $d$  and current  $j$  for different static fields  $E$ . The parameters are  $U = 5$ ,  $g = 1$  and the inverse temperature of the initial state is  $\beta = 5$ .

phonons of frequency  $\omega_0$ , and  $g$  the electron-phonon coupling strength. In a gauge with pure vector potential  $A(t)$ , the electric field  $E(t) = -\partial_t A(t)$  enters via a time-dependent phase for the hopping terms,  $v_{i,j}(t) = v_{i,j}^0 \exp[i(R_i - R_j)A(t)]$ . We will consider an infinite-dimensional hypercubic lattice and apply the field along the body diagonal [26]. The density of states is  $\rho(\epsilon) = \exp(-\epsilon^2/W^2)/\sqrt{\pi}W$ , and we measure energy (time) in units of  $W$  ( $1/W$ ), *i.e.* if the bandwidth of the non-interacting system is 1 eV, the unit of time is about 0.66 fs. Throughout the paper we focus on Mott insulating systems ( $U > \text{bandwidth}$ ) which are strongly coupled to optical phonons with frequencies comparable to the bandwidth ( $\omega_0 = 1$ ). An important parameter to measure the electron-phonon coupling strength is the phonon-mediated attractive interaction  $\lambda = g^2/\omega_0$ , in terms of which the weak-coupling regime corresponds to  $\lambda \ll 1$ .

An approximate treatment of the Holstein-Hubbard model is possible within the framework of nonequilibrium dynamical mean field theory (DMFT) [27–29]. The precise formalism has been detailed in refs. [29,30]. Electric fields can be incorporated via the DMFT self-consistency equations in the same manner as without phonons [28]. To solve the DMFT equations, we use a strong-coupling impurity solver based on the noncrossing approximation [29,31]. This solver has been shown to capture the competition between on-site repulsion and phonon-mediated attraction [29], and is expected to give qualitatively correct results if applied to the Mott phase [31].

**Static fields.** – We first study the dielectric breakdown in a Mott insulating Holstein-Hubbard model with  $U = 5$  and  $g = 1$ . To reduce transients, we smoothly switch on the electric field to the value  $E$  within a time  $t_{\text{switch}} \approx 8$ . Figure 1 plots the time-evolution of the double occupancy  $d(t) = \langle n_{\uparrow}(t)n_{\downarrow}(t) \rangle$  and the current  $j(t) \equiv j_{\sigma} = \langle \frac{1}{L} \sum_k \partial_k \epsilon_{k+A(t)} n_{k\sigma}(t) \rangle$  for different values of  $E$ . At short times and for weak fields, one observes a steady increase in  $d(t)$ , which reflects the field-induced increase of the carrier density. Because these carriers are cooled by phonon-scattering, the current  $j(t)$  increases roughly linearly with the number of carriers (*i.e.* here the phonons

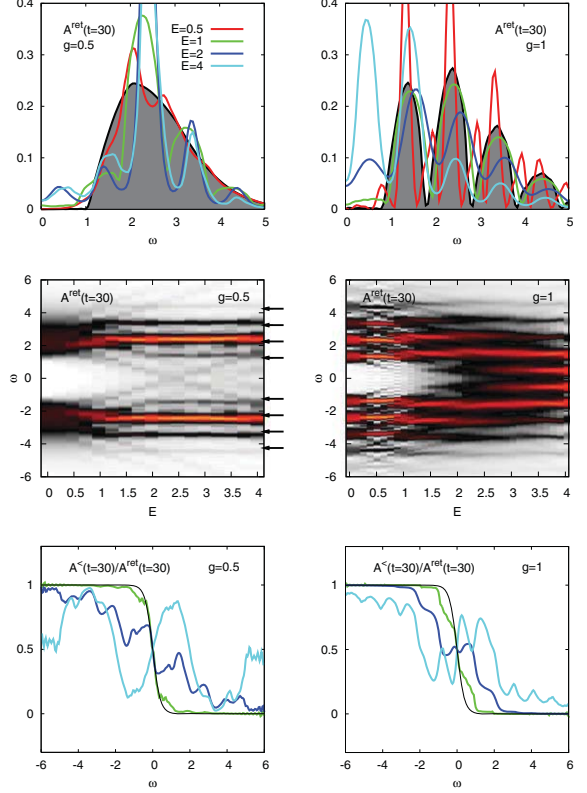


Fig. 2: (Colour on-line) Top four panels: spectral function  $A^{\text{ret}}(\omega, t = 30)$  for  $g = 0.5$  (left) and  $g = 1$  (right), plotted for different values of  $E$  ( $U = 5$ ). The shaded area in the upper panels indicates the spectrum for  $E = 0$  and the arrows in the middle left panel show the positions of the phonon sidebands in the  $E = 0$  spectral function of a model in which the free bandwidth is reduced by a factor of three. Lower panels: “distribution function”  $A^</math>/ $A^{\text{ret}}$  of the quasi-steady state. In black we show the equilibrium distribution functions for  $\beta = 5$ .$

act essentially as a heat bath [5]). For  $E \gtrsim 1.5$  a dielectric breakdown occurs, which is marked by a rapid increase in the current and number of doublons. Despite the strong field, the nonequilibrium Holstein-Hubbard model quickly settles into a quasi-steady state characterized by a large doublon and hole density, and by a large current. In this state, energy is continuously flowing to the lattice. Since the dissipation rate is limited, the quasi-steady current eventually decreases with increasing field [21]. For the largest currents in fig. 1 about 4 phonons per site are excited by  $t = 60$ . (In a real material, anharmonic effects will eventually become important, so that the Hubbard-Holstein description is appropriate only for a sufficiently short time.)

Further insights into the quasi-steady state can be obtained from the nonequilibrium spectral functions  $A^{\text{ret},<}(\omega, t) = \mp \frac{1}{\pi} \int_t^\infty dt' e^{i\omega(t'-t)} \text{Im} G^{\text{ret},<}(t', t)$ . The top four panels in fig. 2 plot  $A^{\text{ret}}(\omega, t = 30)$  for  $g = 0.5$  and  $g = 1$ . The spectrum shows an interplay between field-induced sidebands of the Hubbard bands (Wannier-Stark peaks), whose positions depend linearly on the field, and

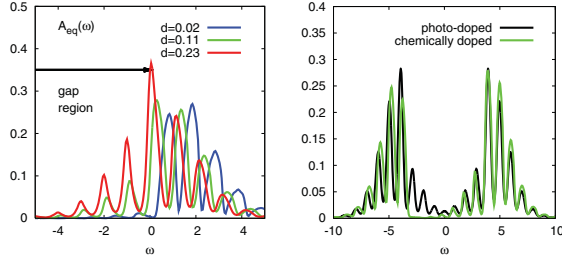


Fig. 3: (Colour on-line) Left panel: equilibrium spectral functions (upper Hubbard band) for the doped Holstein-Hubbard model with  $U = 10, g = 1, \beta = 5$ . Right panel: comparison between the nonequilibrium spectral function of a strongly photo-doped state ( $d = 0.11$  at  $t = 60$ ) and a chemically doped state with a comparable value of  $d$ . The equilibrium spectral function has been shifted to match the position of the dominant peak.

phonon sidebands, which are spaced by  $\omega_0 = 1$  and do not shift with the field. Interestingly, prominent phonon sidebands appear in the presence of an electric field even in the weakly coupled system, where the equilibrium density of states shows no phonon features. The field strength  $E \gtrsim 1$  needed to induce well-separated phonon bands is approximately the same as the field strength which leads to clearly separated Wannier-Stark peaks in the absence of electron-phonon coupling. We thus interpret the observed changes in the spectral function as an effective enhancement of the electron-phonon coupling due to the field-induced localization of the electrons, in analogy to the enhancement of Coulomb interaction effects in the Wannier-Stark states in metals [32,33]. In fact, the field-induced phonon sidebands resemble the phonon sidebands which appear in equilibrium calculations with a reduced bandwidth (see arrows in the middle left panel of fig. 2). The main difference is that the sideband below the dominant peak is more prominent in the nonequilibrium case and that the peaks are shifted to slightly higher energy.

In the strong-coupling regime ( $g = 1$ , right panels of fig. 2) the Hubbard bands are split into phonon sidebands already in the thermal initial state. Here, one observes Wannier-Stark sidebands emanating from the phonon peaks already at weak fields. The Wannier-Stark bands intersect at fields  $E \approx n\omega_0 + 0.5$  ( $n = 0, 1, \dots$ ), leading to much sharper phonon sidebands due to field-induced localization, while the phonon bands broaden around the resonances  $E \approx n\omega_0$  ( $n = 1, 2, \dots$ ). For field strengths larger than the gap size ( $E \gtrsim 1.5$ ) one notices the appearance of states in the gap region. These in-gap states correspond to polarons (doublons or holes dressed by phonons). They are highly occupied for  $\omega > 0$  (dressed doublons) and depleted for  $\omega < 0$  (dressed holes), as apparent from a partial inversion of the “nonequilibrium distribution function”  $A^<(\omega, t = 30)/A^{\text{ret}}(\omega, t = 30)$  in the gap region (fig. 2, bottom panels).

The field-induced in-gap states are reminiscent of the sidebands appearing in the equilibrium spectral functions

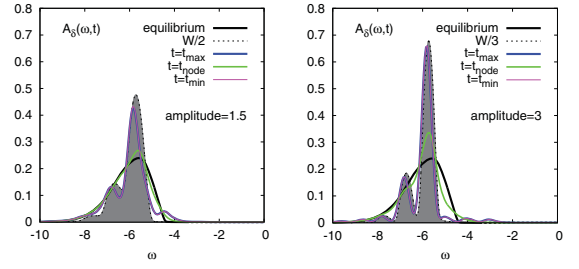


Fig. 4: (Colour on-line) Time-resolved photo-emission spectrum  $A_\delta(\omega, t)$  for probe-pulse width  $\delta = 4$  in a system driven by a slow  $\Omega_{\text{pulse}} = 0.0833$  single-cycle pulse with amplitude much smaller than the gap ( $U = 12, g = 0.5$ ). The measurements are taken at the maximum of the first half-cycle ( $t = t_{\text{max}} = 21.8$ ), at the node ( $t = t_{\text{node}} = 31.4$ ) and at the minimum of the second half-cycle ( $t = t_{\text{min}} = 41.1$ ). The grey spectra are equilibrium results for a model with reduced bandwidth  $W/2$  (left) and  $W/3$  (right).

of doped Mott insulators. To show this, we plot in the left panel of fig. 3 the upper Hubbard band of electron-doped systems with  $U = 10, g = 1, \beta = 5$ . As the number of doublons increases, prominent sidebands (corresponding to electron-like polarons) appear in the gap region.

**Slow (THz) pulse.** – The effective enhancement of the electron-phonon coupling might be observable in Mott insulators driven by a slow (quasi-DC) field pulse. To illustrate this, we plot in fig. 4 the time-resolved photo-emission spectrum [34]  $A_\delta(\omega, t_p) = -i \int dt dt' s(t - t_p) s(t' - t_p) e^{i\omega(t-t')} G^<(t, t')$ , measured with a Gaussian probe pulse envelope  $s(t) = \exp(-t^2/\delta^2)$ . We consider a large gap insulator with relatively weak phonon coupling ( $U = 12, g = 0.5$ ), which is driven by a single-cycle field pulse with frequency  $\Omega_{\text{pulse}} = 0.0833 \ll \text{gap}$ . The low frequency of the pulse prevents photo-doping, while the large  $U$  allows us to apply peak fields comparable to the width of the Hubbard bands while remaining well below the dielectric breakdown value. The curves in the figure show the photo-emission spectrum measured near the maximum ( $t = t_{\text{max}}$ ), the minimum ( $t = t_{\text{min}}$ ), and the node ( $t = t_{\text{node}}$ ) of the pump pulse. The width of the probe pulse ( $\delta = 4$ ) is chosen such that the field-induced phonon sidebands can be resolved in frequency, while the spectra measured at  $t = t_{\text{max}}, t_{\text{min}}$  and  $t_{\text{node}}$  can be clearly separated in time. Already for a pump pulse amplitude of 1.5 one can clearly identify the field-induced phonon sidebands in the spectra measured near the maxima of the pump pulse, while the spectrum near the node differs only little from the featureless equilibrium result<sup>1</sup>. At the larger field amplitude of 3, the phonon features are even more prominently visible. In both cases, the pump pulse produces only a negligible number of doublons,  $O(10^{-6})$ , so that the spectra measured at the first maximum and

<sup>1</sup>Taking parameters for  $\text{Cs}_3\text{C}_{60}$  (bandwidth of 0.4 eV, lattice spacing of 15 Å [15]) the peak field strengths used in our calculations are of  $O(10^6)$  V/cm.

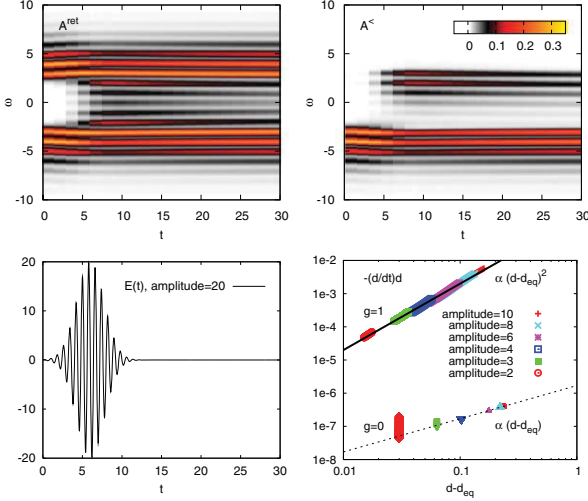


Fig. 5: (Colour on-line) Top panels: time-resolved spectral function  $A^{\text{ret}}(\omega, t)$  (left) and  $A^<(\omega, t)$  (right) after a pulse excitation ( $U = 8, g = 1$ ). Bottom left panel: few-cycle pulse with  $\Omega_{\text{pulse}} \approx 8$ . Bottom right panel: doublon decay rate as a function of  $d - d_{\text{eq}}$  for different pulse amplitudes (photo-doping concentrations).

the first minimum are almost identical. Again, we find that the nonequilibrium spectra are qualitatively similar to equilibrium spectra for a reduced bandwidth (see gray spectra in fig. 4), which confirms that the main effect is a field-induced localization of the electrons<sup>2</sup>.

**Photo-doping.** – Nonthermal spectral functions with polaronic mid-gap states also appear after photo-doping. We first analyze this effect for a Mott insulator with  $U = 8$  and a few-cycle electric field pulse with frequency  $\Omega_{\text{pulse}} \approx 8$ . This pulse excites electrons across the gap and creates a population in the middle of the upper Hubbard band. In the absence of electron-phonon coupling the occupied part of the spectral function relaxes very slowly [20] and there is little change in the total spectral function. In the Holstein-Hubbard model, the photo-doping leads to modifications in the spectral function, which depend strongly on the concentration of carriers. For  $g = 1$ , polaronic in-gap states appear, which are populated by doublons for  $\omega > 0$  and by holes for  $\omega < 0$  (fig. 5). The spectral features of a photo-doped system are almost identical to those of a chemically doped system with comparable doublon density (see right panel of fig. 3), which indicates that the cooling by the phonons is effective and that we can view the photo-doped state as a “cold” state in the subspace of the Hilbert space corresponding to a certain number of doublons and holes.

The formation of polaronic in-gap states has profound effects both on the relaxation and on the recombination of

<sup>2</sup>Besides the dominant band-narrowing effect, a quasi-static field also leads to an enhanced electronic self-energy  $|\text{Im}\Sigma^R(t, t)|$  and a shift of spectral weight  $\text{Im}\Sigma^R(\omega, t)$  to higher energies. Using sum rules [35], this change can be related to enhanced fluctuations in the phonon position.

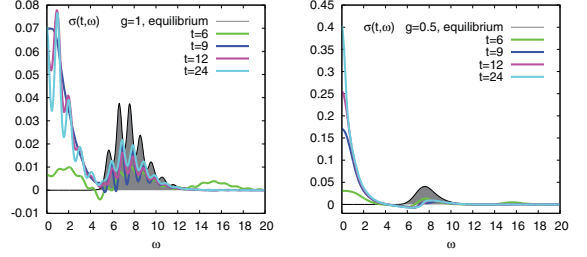


Fig. 6: (Colour on-line) Time-resolved optical conductivity after a pulse excitation. Left panel:  $U = 8, g = 1$ . Pulse form as in fig. 5, but with amplitude 8. The doublon number  $d - d_{\text{eq}}$  for  $t = 9, 12, 24$  is 0.16, 0.15, 0.11 ( $g = 1$ ) and 0.21, 0.22, 0.21 ( $g = 0.5$ ).

photo-excited carriers. In the absence of electron-phonon coupling, the life-time  $\tau$  of photo-doped carriers (from  $d(t) \sim \exp(-t/\tau)$ ) is slow and depends exponentially on the gap size [20,36]. For large  $g$ , the doping-induced in-gap states lead to a doping-dependent doublon-hole life-time. If we plot the recombination rate  $(-d/dt)d$  as a function of doublon concentration<sup>3</sup>  $d - d_{\text{eq}}$  for different pulse amplitudes (doping concentrations), we find that the rate grows with the concentration approximately like  $(d - d_{\text{eq}})^2$ , see bottom right panel of fig. 5. This quadratic dependence indicates that the rate is determined by the probability of electron-like polarons meeting hole-like polarons, which is entirely different from the kinetically blocked, exponentially slow decay in the Hubbard model. (The decay rate for  $g = 0$  scales linearly with  $d - d_{\text{eq}}$ .)

The formation of a metallic state with polaronic carriers after a photo-doping pulse is also evident in the time-resolved optical conductivity. This is not surprising, because within DMFT, the optical conductivity  $\sigma(\omega, t)$  (whose definition is given in ref. [37]) is obtained from the convolution of two time-dependent spectral functions. Figure 6 shows  $\sigma(\omega, t)$  for the pulse-excited system with  $U = 8, g = 1$  and  $g = 0.5$ . The pulse shape is the same as that shown in fig. 5, but with a smaller amplitude. In the initial equilibrium state ( $\beta = 5$ ), the optical conductivity has weight around  $\omega = 8$ , corresponding to transitions between the Hubbard bands, which for the larger phonon-coupling are split into phonon sidebands. At  $t = 6$ , during the application of the pulse with frequency  $\Omega_{\text{pulse}} \approx 8$ , the conductivity in the low-energy region grows, and we notice some weight also at energy  $\omega \approx 16$  (for simplicity, we have neglected vertex corrections, which may be relevant in the presence of an external field). This high-energy feature may correspond to “Floquet sidebands”, which are separated from the Hubbard bands by multiples of the driving frequency  $\Omega_{\text{pulse}}$  [38]. At  $t = 9$  the pulse is over and this high-energy feature is gone. Instead, a Drude peak appears at low frequencies. Because of the cooling effect, the peak in the model with weak phonon coupling

<sup>3</sup>We use the double occupancy in the initial equilibrium state as an estimate for  $d_{\text{eq}}$ .



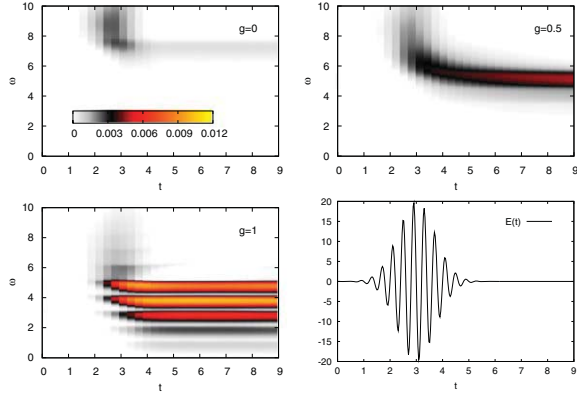


Fig. 7: (Colour on-line) Time-resolved spectral function  $A^{\text{ret}}$  during and shortly after a pulse excitation. The interaction is  $U = 12$  and the pulse frequency is  $\Omega_{\text{pulse}} \approx 15$  (*i.e.* doublons are inserted at the upper edge of the Hubbard band).

( $g = 0.5$ ) grows and sharpens on a timescale of about  $20/W$ , indicating the formation of a metallic state with large kinetic energy. In the model with  $g = 1$ , the growth of the Drude peak stops already at  $t \approx 9$ , and its weight is considerably smaller than in the weakly coupled case<sup>4</sup>. At later times  $\omega_0$ -periodic modulations appear in the Drude peak, which arise from transitions between the partially filled polaronic sidebands. Since the polaronic features are clearly visible in the time-resolved optical conductivity, we expect that the field-induced enhancement of the electron-phonon coupling, as evidenced for example by the proposed sub-gap THz pump experiment (fig. 4), can also be detected in optical conductivity data.

**Dissipation.** – To illustrate the cooling of the photo-doped carriers due to electron-phonon scattering we consider a large-gap insulator ( $U = 12$ ) subject to an intensive few-cycle pulse with  $\Omega_{\text{pulse}} \approx 15$ , which creates a population at the upper edge of the upper band (a larger value of  $U$  is chosen here to suppress the doublon-hole recombination on the timescale of the plot). Plots of  $A^<(\omega, t)$  for different values of  $g$  are shown in fig. 7. In the absence of electron-phonon coupling only a small number of doublons is inserted (due to the small overlap of the upper Hubbard band with the power spectrum of the pulse), and these photo-doped carriers remain confined to the upper edge of the band up to times  $t \gg 10$ . For  $g = 0.5$ , the spectral weight shifts to lower energies and piles up at the lower band edge already at  $t \approx 8$ . For weak coupling, the relaxation (energy dissipation rate) can be estimated from the drift velocity of the spectral weight from the upper band edge to the lower band edge. For even larger electron-phonon coupling the Hubbard bands broaden due to pronounced phonon sidebands and the appearance of in-gap states. In the simulation for  $g = 1$  one observes

<sup>4</sup>The main reason for this is that the kinetic energy of the polarons is lower. While the doublon density is lower in the calculation with  $g = 1$  by a factor of less than two, see caption of fig. 6, this fact alone cannot explain the differences in the Drude peak.

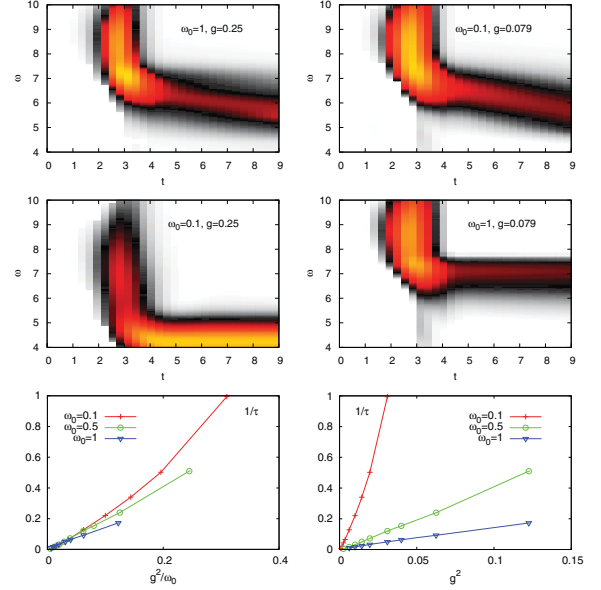


Fig. 8: (Colour on-line) Top four panels: occupied spectral weight  $A^<(t, \omega)$  in the upper Hubbard band of a photo-doped system with  $U = 12$  and indicated values of  $g$  and  $\omega_0$  (different arbitrary intensity scales). The parameters in the top two panels correspond to the same  $g^2/\omega_0$ . Bottom panels: relaxation time  $\tau$  extracted from the kinetic energy plotted as a function of  $g^2$  (right panel) and  $g^2/\omega_0$  (left panel).

a rapid population of these sidebands by the cooled polarons. The cooling of photo-induced doublons from an energy  $\Omega/2 \approx 7.5$  to the lowest phonon-peaks in the upper Hubbard band ( $\omega \approx 4$ ) occurs already during the application of the pulse (before  $t = 4$ ), and the subsequent relaxation and polaron-formation (appearance of doping-induced in-gap states) is also a very fast process.

Our numerical simulations show that neither  $\omega_0$ , nor the coupling strength  $g$  individually determine this dissipation strength, but the parameter  $\lambda = g^2/\omega_0$ . The top two panels of fig. 8 plot  $A^<(\omega, t)$  in two systems with  $U = 12$ , but very different phonon frequencies and phonon coupling strengths. The parameters,  $\omega_0 = 1, g = 0.25$  and  $\omega_0 = 0.1, g = 0.079$  however correspond to the same  $g^2/\omega_0$ . While the density of absorbed doublons is different in the two simulations, the drift velocity of the spectral weight is almost identical. In contrast, the model with  $\omega_0 = 0.1, g = 0.25$  ( $\omega_0 = 1, g = 0.079$ ) shows a much faster (slower) relaxation (see middle panels). From the approximately exponential long-time relaxation of the kinetic energy we can furthermore extract relaxation times  $\tau$ . The bottom right panel plots  $1/\tau$  as a function of  $g^2$  for different  $\omega_0$ . While for fixed  $\omega_0$ ,  $1/\tau$  grows approximately proportional to  $g^2$ , it depends strongly on the value of the phonon frequency. A rough data collapse is obtained if we plot  $1/\tau$  as a function of  $g^2/\omega_0$  (bottom left panel).

Finally, the spectral weight plots in fig. 7, which use the same intensity scale, suggest that the number of carriers produced by the high-frequency pulse is enhanced by the

phonon coupling. We analyzed the  $g$ -dependence of the doping concentration, and compared it with the result expected for a rigid spectral function which does not respond to the pulse. If the field-strength is in the linear regime, we expect a number of doped carriers proportional to the convolution  $N_{\text{naive}} = \int d\omega' d\omega A^{\text{ret}}(\omega) p(\omega) A^{\text{ret}}(\omega - \omega') f(\omega - \omega')(1 - f(\omega))$ , where  $p(\omega)$  is the power spectrum of the pulse and  $f(\omega)$  is the Fermi distribution function for  $\beta = 5$ . While  $N_{\text{naive}}$  increases by a factor 1.7 if  $g$  is increased from 0 to 1, due to the broadening of the spectral function, the number of doped carriers in the linear regime increases by a factor of about 4.4. For pulse amplitude 20, outside the linear regime (fig. 7), the corresponding increase is by a factor 17.

**Conclusions.** – We have shown that field-induced carriers in the Holstein-Hubbard model cool down through the interaction with phonons and form polaronic states, which leads to characteristic changes in the time-resolved photo-emission spectrum. The appearance of dressed electron- and hole-like carriers also has a significant effect on the carrier recombination time. Even without doublon-hole production, electric fields can induce polaronic features because the electron localization in strong fields reduces the bandwidth and effectively enhances the parameter  $\lambda = g^2/\omega_0$  which controls the influence of the phonons. These effects may be observable in time-resolved photo-emission measurements or optical conductivity measurements on organic Mott insulators, such as  $\text{Cs}_3\text{C}_{60}$ . Spectral changes related to the polaronic in-gap states discussed in this work may in fact have been observed in recent experiments on cuprates [39] and one-dimensional Mott insulators [18].

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