

# Photon cascade emission in Pr<sup>3+</sup> doped fluorides with CaF<sub>2</sub> structure: Application of a model for its prediction

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In this work, we predict and measure the optical behaviour of Pr<sup>3+</sup> in different binary and ternary fluorides. We use a validated model based on Ligand Field Theory and Density Functional Theory to calculate the multiplet energy levels arising from the ground [Xe]4f<sup>2</sup> and excited [Xe]4f<sup>1</sup>5d<sup>1</sup> electron configurations of Pr<sup>3+</sup> in its chemical environment. Moreover, the luminescence spectra of the considered materials were recorded. In overall the theoretical determination corroborates to the experimental findings. The phenomenon of the photon cascade emission is particularly stressed, being important for the design of modern phosphors with quantum efficiencies larger than 100%.

## 1. Introduction

Divalent and trivalent lanthanide ions are widely applied in phosphors, laser gain media and scintillator crystals or ceramics. Especially trivalent praseodymium (Pr<sup>3+</sup>) shows a large variety of different applications as activator ion, viz. UV phosphors [1], laser materials [2], up- [3] and down-conversion [4,5] phosphors. The down-conversion phosphors also called quantum cutter systems or photon cascade emission materials (PCE), exhibit a two or more photon luminescence process, where at least two low energy photons are emitted per one high energy photon absorbed [6,7]. Therefore, quantum efficiencies larger than 100% are achievable. PCE materials can be useful in plasma display panels or Hg-free discharge lamps, in which the phosphors are excited by vacuum UV radiation from the Xe excimer discharge [8].

The observation of PCE in Pr<sup>3+</sup> phosphors was simultaneously described by Sommerdijk et al. [4] and by Piper et al. [5] in 1974 for YF<sub>3</sub>. There Piper et al. reported quantum efficiencies of about 140%, which have also been found for β-NaLaF<sub>4</sub> [9]. Aside the usual fluoride hosts, Pr<sup>3+</sup> doped oxidic hosts, viz. SrAl<sub>12</sub>O<sub>19</sub> [10], LaMgB<sub>5</sub>O<sub>10</sub> [11], and LaB<sub>3</sub>O<sub>6</sub> [12] were demonstrated to show PCE, whose phenomenon can only be observed if the lowest energy level of the excited [Xe]4f<sup>1</sup>5d<sup>1</sup> electron configuration of Pr<sup>3+</sup> is located above the <sup>1</sup>S<sub>0</sub> energy level of the ground [Xe]4f<sup>2</sup> electron

configurations [5]. It is of crucial importance to delimitate the multiplet energy levels arising from the ground [Xe]4f<sup>2</sup> and the excited [Xe]4f<sup>1</sup>5d<sup>1</sup> electron configurations of Pr<sup>3+</sup> in its chemical environment. It turns out that an overlap between both multiplet energy levels is controlled by a balance between two interactions such as the nephelauxetic effect and the ligand field splitting [13].

Since fluoride ligands exhibiting a small nephelauxetic effect [13], the position of the lowest energy level of the [Xe]4f<sup>1</sup>5d<sup>1</sup> configuration depends mainly on the ligand field splitting of the 5d orbitals. This ligand field splitting is mainly dependent on the coordination sphere of the Pr<sup>3+</sup> ion.

We consider herein four different host matrices, (CaF<sub>2</sub>, SrF<sub>2</sub>, BaF<sub>2</sub>, and α-NaYF<sub>4</sub>) all crystallizing in the cubic CaF<sub>2</sub> structure type (space group *Fm*–*3m*). The Pr<sup>3+</sup> is doped in the unique eight-fold coordinated cation site having O<sub>h</sub> symmetry [14]. The cubic α-phase of NaYF<sub>4</sub> is the high-temperature polymorph, unlike the low temperature one which possesses the hexagonal (space group *P*–*6*) β-phase [15]. In α-NaYF<sub>4</sub> the cation site is randomly occupied by ½ Na<sup>+</sup> and ½ Y<sup>3+</sup> [16].

The luminescence of these Pr<sup>3+</sup> activated fluorides has been experimentally described by several working groups [17–19]. The alkaline earth fluorides (CaF<sub>2</sub>:Pr<sup>3+</sup>, SrF<sub>2</sub>:Pr<sup>3+</sup>, and BaF<sub>2</sub>:Pr<sup>3+</sup>) show in all the cases broad band emission due to the fact that the lowest energy level of the [Xe]4f<sup>1</sup>5d<sup>1</sup> configuration is located below the <sup>1</sup>S<sub>0</sub> energy level [17]. Thus the ligand field splitting of the 5d orbitals is expected to be large. On the other hand, the α-NaYF<sub>4</sub>:Pr<sup>3+</sup> shows line emission proper for PCE materials [18,19]. Here the ligand field interaction of the 5d orbitals is certainly weaker. These findings

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cannot be solely explained by the different sizes of the replaced cations,  $\text{Ca}^{2+}$ : 126 pm,  $\text{Sr}^{2+}$ : 140 pm,  $\text{Ba}^{2+}$ : 156 pm and  $\text{Y}^{3+}$ : 116 pm in contrast to  $\text{Pr}^{3+}$ : 126.6 pm (all given for coordination number (CN) 8 [20]), since the chemical environment and the symmetry is in all cases identical. Rodnyi et al. [21] reported about the energy shift of the lowest level of the  $[\text{Xe}]4f^1 5d^1$  configuration as function of the  $\text{Pr}^{3+}$  concentration in  $\text{BaF}_2$  crystals. For higher concentrations (3.0%) PCE was observed due to the formation of  $\text{Pr}^{3+}$ -based clusters.

Here we apply our validated model [13] to explain and predict the above mentioned PCE phenomenon. This model is also essential for tailoring phosphors to generate warm-white light [22]. The structure of the  $\text{Pr}^{3+}$  doped systems is optimized using periodical calculations based on Density Functional Theory (DFT) by means of the VASP code [23,24]. The PBE functional is used to parameterize the exchange-correlation potential [25]. The structure of the doped system is obtained taking into account a super-cell model composed by one  $\text{Pr}^{3+}$  ion in 32 unit-cells corresponding to a dopant concentration of 3%. It is important to mention that the  $\text{Pr}^{3+}$  ions are handled as isolated ions. A selective cut of this optimized structure is performed taking into account the  $\text{Pr}^{3+}$  centre and its surrounding ligands, subjected to a molecular calculation using the Amsterdam Density Functional (ADF 2013.01) program package [26,27]. We use the computational model named LFDFT [13,28,29], whose output enables the computations of the Slater-Condon parameters, spin-orbit coupling constants and ligand field potential. Preparation and optical characterization of  $\text{CaF}_2:\text{Pr}^{3+}, \text{Na}^+$ ;  $\text{SrF}_2:\text{Pr}^{3+}, \text{Na}^+$ ;  $\text{BaF}_2:\text{Pr}^{3+}, \text{Na}^+$ ; and  $\alpha\text{-NaYF}_4:\text{Pr}^{3+}$  are performed (see Section 4). The doping level was in all cases adjusted to 1.0% to avoid clustering of  $\text{Pr}^{3+}$  in the powder samples. The prepared phosphors were of single phase and luminescence spectra were recorded from the VUV to the near infrared region.

## 2. Results and discussion

The calculations for the  $\text{Pr}^{3+}$  doped alkaline earth fluorides and  $\alpha\text{-NaYF}_4$  yield the parameters listed in Table 1. In the table two columns are devoted to the  $\alpha\text{-NaYF}_4$  system relating the two special extreme situations which are illustrated by taking the second coordination sphere containing exclusively  $\text{Na}^+$  (hereafter  $\text{O}_h(\text{Na})$ )

**Table 1**

Electrostatic and ligand field parameters for all  $\text{Pr}^{3+}$  doped hosts with  $\text{O}_h$  site symmetry (in  $\text{cm}^{-1}$ ).

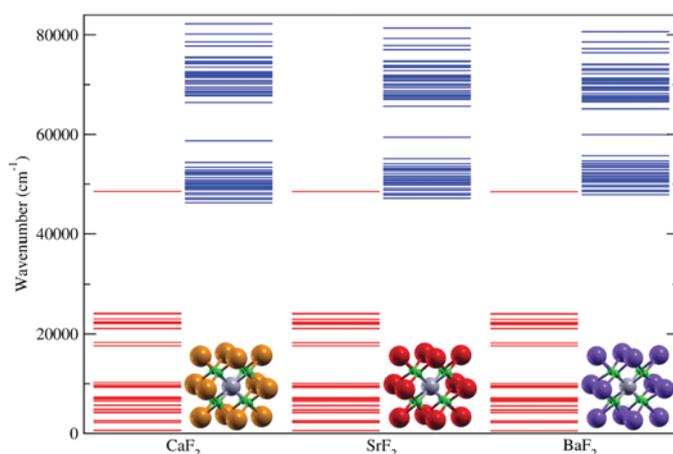
Host Symmetry	$\text{CaF}_2$ $\text{O}_h$	$\text{SrF}_2$ $\text{O}_h$	$\text{BaF}_2$ $\text{O}_h$	$\alpha\text{-NaYF}_4$ $\text{O}_h(\text{Na})$	$\alpha\text{-NaYF}_4$ $\text{O}_h(\text{Y})$
$F_2(\text{ff})^a$	322.8	322.9	322.9	322.9	322.8
$F_4(\text{ff})^a$	41.7	41.7	41.7	41.7	41.7
$F_6(\text{ff})^a$	4.4	4.4	4.4	4.4	4.4
$G_1(\text{fd})^a$	358.9	356.9	351.2	350.2	365.3
$F_2(\text{fd})^a$	226.7	225.3	222.7	221.4	229.4
$G_3(\text{fd})^a$	30.7	30.5	30.1	29.9	31.2
$F_4(\text{fd})^a$	17.4	17.3	17.1	17.0	17.6
$G_5(\text{fd})^a$	4.8	4.7	4.7	4.7	4.9
$\zeta_{4f}^b$	710	710	710	710	710
$\zeta_{5d}^b$	945	945	945	945	945
$e_\sigma(\text{f})^c$	599	538	491	450	673
$e_\pi(\text{f})^c$	257	232	213	164	279
$e_\sigma(\text{d})^c$	14 114	13 009	12 154	11 652	16 210
$e_\pi(\text{d})^c$	4705	4336	4051	3886	5404
$\Delta_{\text{AOM}}(\text{fd})^d$	15 183	17 918	20 030	21 162	9851

<sup>a</sup>  $F_k(\text{ff})$ ,  $F_k(\text{fd})$  and  $G_k(\text{fd})$  refer to the interelectronic effect known as Slater-Condon parameters widely described in textbooks [30,31].

<sup>b</sup> Spin-orbit coupling constants for the 4f and 5d orbitals were obtained using the relativistic ZORA approach [13].

<sup>c</sup> The ligand field interaction is better represented with respect to the Angular Overlap Model (AOM) parameters [32]. In the present case four AOM parameters are available due to the problem of two-open-shell 4f and 5d electrons.

<sup>d</sup> We refer to [32] and define  $\Delta_{\text{AOM}}(\text{fd})$  accordingly.



**Figure 1.** Calculated multiplet energy levels of  $\text{Pr}^{3+}$  doped  $\text{CaF}_2$ ,  $\text{SrF}_2$ , and  $\text{BaF}_2$  corresponding to the  $[\text{Xe}]4f^2$  (red) and the  $[\text{Xe}]4f^1 5d^1$  configurations (blue). The structures represent the central  $\text{Pr}^{3+}$  ion (grey) surrounded by eight  $\text{F}^-$  (green) and the second coordination sphere containing the corresponding alkaline earth cations. (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

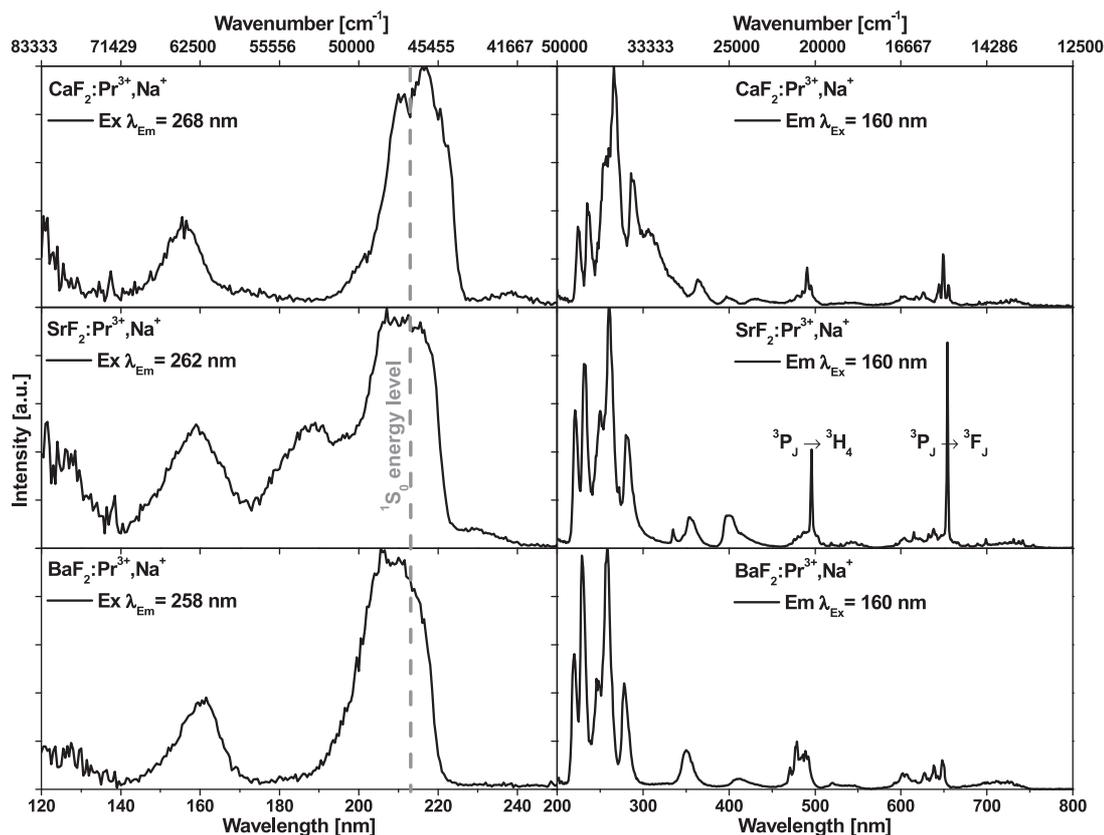
or  $\text{Y}^{3+}$  (hereafter  $\text{O}_h(\text{Y})$ ) ions. In both situations,  $\text{O}_h$  symmetry of the coordination of the  $\text{Pr}^{3+}$  is achieved.

The theoretical results are graphically represented in Figure 1, where the multiplet energy levels originating from the  $[\text{Xe}]4f^2$  and the  $[\text{Xe}]4f^1 5d^1$  configurations are given in red and blue, respectively. An overlap between both multiplet energy levels is noticed. Thus PCE is not observed as it is confirmed by our related experimental work (see Figure 2) which is also in line with earlier observations by Lawson et al. [17].

Due to the weak ligand field interaction of the 4f orbitals of  $\text{Pr}^{3+}$  (see parameters in Table 1), in Figure 1 the multiplet energy levels arising from the  $[\text{Xe}]4f^2$  configurations seem to be identical in any systems. On the other hand, the influence of the chemical surrounding on the 5d orbitals is stronger which results in a different splitting of the  $[\text{Xe}]4f^1 5d^1$  configurations. In the present situation the 5d orbitals of  $\text{Pr}^{3+}$  split over  $e_g$  and  $t_{2g}$  irreducible representations of the  $\text{O}_h$  point group. Therefore, the multiplet energy levels from the  $[\text{Xe}]4f^1 5d^1$  configurations are split in two different bands fully recognized in Figure 1 but also in the experimental characterization below (see Figure 2).

The ionic radii of  $\text{Ca}^{2+}$  (126 pm) and  $\text{Pr}^{3+}$  (126.6 pm) for CN 8 are almost identical, whereas the ionic radii of  $\text{Sr}^{2+}$  (140 pm) and  $\text{Ba}^{2+}$  (156 pm) are much larger. This means, that the size of the cation which is replaced by  $\text{Pr}^{3+}$  is increasing (see Table 2) in the series of  $\text{CaF}_2$ ,  $\text{SrF}_2$  and  $\text{BaF}_2$  leading to a decrease of the splitting for the 5d orbitals of  $\text{Pr}^{3+}$ . The total splitting of the calculated multiplet energy levels between  $e_g$  and  $t_{2g}$  is specified with  $20 910 \text{ cm}^{-1}$  for  $\text{CaF}_2:\text{Pr}^{3+}$ ,  $19 272 \text{ cm}^{-1}$  for  $\text{SrF}_2:\text{Pr}^{3+}$ , and  $18 006 \text{ cm}^{-1}$  for  $\text{BaF}_2:\text{Pr}^{3+}$ .

The luminescence spectra of the  $\text{Pr}^{3+}$  doped alkaline earth fluorides are measured (see Section 4) and given in Figure 2. Since we focus on the lowest energy level of the  $[\text{Xe}]4f^1 5d^1$  configuration, excitation spectra were monitored in the VUV part of the spectral range. The excitation spectra indicate that there are two separated bands which can be compared to the  $e_g$  and  $t_{2g}$  levels known for  $\text{O}_h$  symmetry. The splitting between these two bands is decreasing from about  $18 230 \text{ cm}^{-1}$  for  $\text{CaF}_2:\text{Pr}^{3+}, \text{Na}^+(1.0\%)$  and  $14 580 \text{ cm}^{-1}$  for  $\text{SrF}_2:\text{Pr}^{3+}, \text{Na}^+(1.0\%)$  to  $13 260 \text{ cm}^{-1}$  for  $\text{BaF}_2:\text{Pr}^{3+}, \text{Na}^+(1.0\%)$ . The values were derived taking the energy difference between the two maxima of the excitation bands, whereas it is important to announce that the measurements were done at room temperature (298 K). Our theoretical results overestimate them by about 20%, although the case of  $\text{CaF}_2:\text{Pr}^{3+}$  are perfectly in line with the



**Figure 2.** Room temperature luminescence spectra of  $\text{CaF}_2:\text{Pr}^{3+},\text{Na}^+(1.0\%)$ ,  $\text{SrF}_2:\text{Pr}^{3+},\text{Na}^+(1.0\%)$  and  $\text{BaF}_2:\text{Pr}^{3+},\text{Na}^+(1.0\%)$ . VUV excitation spectra are plotted on the left and emission spectra on the right. The dashed grey line represents the energy position of the  $^1\text{S}_0$  energy level.

observation of Oskam et al. [35]. They reported a ligand field splitting of the 5d orbitals of about  $21\,000\text{ cm}^{-1}$  derived from experimental work (measured at 6 K). The discrepancy originates from the temperature dependence of the  $t_{2g}$  levels, meanwhile the  $e_g$  levels remain at the same energy. This was already observed by Loh [36] in former investigations of the UV absorption of  $\text{Pr}^{3+}$  doped alkaline earth fluorides. Since the  $e_g$  levels remain at the same energy, changes in the emission spectra cannot be observed. The highest energy level  $^1\text{S}_0$  of the ground  $[\text{Xe}]4f^2$  configuration is expected to be located close to  $47\,000\text{ cm}^{-1}$  as it is determined theoretically (see Figure 1) and which was already described in literature [4,35]. Therefore, the lowest energy level of the  $[\text{Xe}]4f^15d^1$  configuration is in all cases overlapping with the highest energy level  $^1\text{S}_0$ . PCE for these phosphors is not observed whereby the emission spectra in Figure 2 mainly show broad band emission from the lowest energy level of the  $[\text{Xe}]4f^15d^1$  configuration in the UV part of the spectral range. In case of  $\text{SrF}_2:\text{Pr}^{3+},\text{Na}^+$  an intermediate band between the  $e_g$  and the  $t_{2g}$  ones appears which is due to a small amount of residual  $\text{PrF}_3$  [37]. However, this leads to higher intensities of intraconfigurational  $[\text{Xe}]4f^2-[\text{Xe}]4f^2$  transitions which can only be observed in the case of  $\text{SrF}_2:\text{Pr}^{3+},\text{Na}^+$ .

In comparison to the binary alkaline earth fluorides the ternary  $\alpha\text{-NaYF}_4$  is investigated. The  $\alpha$ -polymorph exhibits the cubic  $\text{CaF}_2$  structure type with  $\text{Na}^+$  and  $\text{Y}^{3+}$  randomly distributed on the cation

sites. Here, the average bond length is comparable to the one of  $\text{CaF}_2$  (see Table 2).

The results of the calculations are given in Figure 3, following the same representations as in Figure 1. The two above mentioned extreme situations of the  $\text{O}_h$  symmetry are calculated separately. An overlap between both multiplet energy levels is noticed again. Thus PCE is not expected in both situations which is in contradiction to our experimental results (see Figure 4) and also to the experimental work published by Sommerdijk et al. [18].

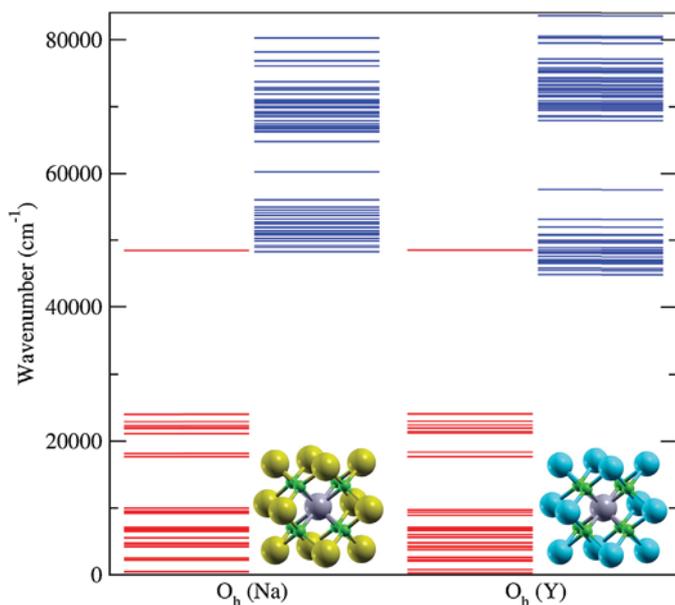
The multiplet energy levels arising from the  $[\text{Xe}]4f^2$  configurations in Figure 3 seem to be again nearly identical for the two different  $\text{O}_h$  situations. The influence of the chemical surrounding on the 5d orbitals is much stronger which results in a different splitting for the  $[\text{Xe}]4f^15d^1$  configurations.  $\text{Na}^+$  has a larger ionic radius than  $\text{Y}^{3+}$ , leading to smaller splitting of the 5d orbitals of  $\text{Pr}^{3+}$ . Therefore, the lowest energy level of the  $[\text{Xe}]4f^15d^1$  configuration is located at higher energy but still below the  $^1\text{S}_0$  energy level. The total splitting of the calculated multiplet energy levels between  $e_g$  and  $t_{2g}$  is specified with  $17\,255\text{ cm}^{-1}$  for  $\text{O}_h(\text{Na})$  and  $24\,015\text{ cm}^{-1}$  for the  $\text{O}_h(\text{Y})$  symmetry.

The luminescence spectra of  $\alpha\text{-NaYF}_4:\text{Pr}^{3+}(1.0\%)$  are given in Figure 4. The excitation spectrum shows one broad band ranging from  $48\,000$  to  $72\,000\text{ cm}^{-1}$  with two next neighboured maxima. The highest energy level  $^1\text{S}_0$  of the ground  $[\text{Xe}]4f^2$  configuration is

**Table 2**

Cation-anion bond length in different hosts (in pm). Literature values give the bond length of the undoped hosts whereas the calculated ones display the values of the theoretical  $\text{Pr-F}$  bond. In case of  $\alpha\text{-NaYF}_4$  the distance from the literature shows the average value.

Host	$\text{CaF}_2$	$\text{SrF}_2$	$\text{BaF}_2$	$\alpha\text{-NaYF}_4$	$\alpha\text{-NaYF}_4$
Symmetry	$\text{O}_h$	$\text{O}_h$	$\text{O}_h$	$\text{O}_h(\text{Na})$	$\text{O}_h(\text{Y})$
Literature (undoped)	236.6 [33]	251.1 [33]	268.5 [33]	235.7 [34]	235.7 [34]
Calculated (doped)	237.2	240.9	244.0	245.7	231.8

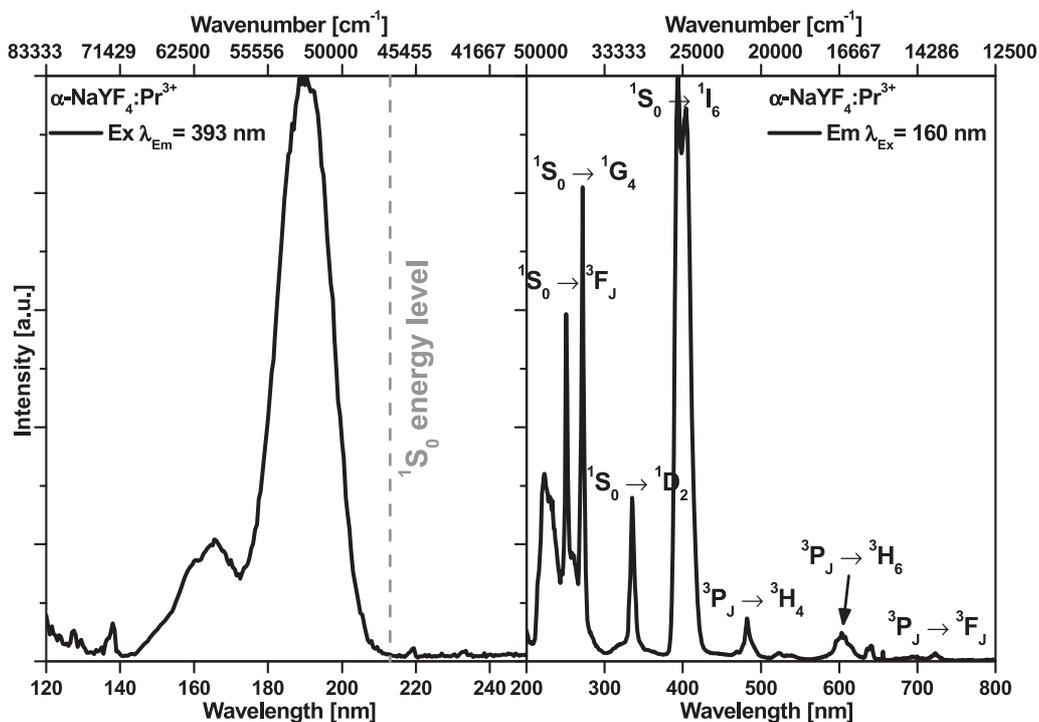


**Figure 3.** Calculated multiplet energy levels of  $\text{Pr}^{3+}$  doped  $\alpha\text{-NaYF}_4$ , corresponding to the  $[\text{Xe}]4f^2$  (red) and the  $[\text{Xe}]4f^1 5d^1$  configurations (blue). The two given symmetries differ in the second coordination sphere containing just  $\text{Na}^+$  ( $\text{O}_h(\text{Na})$ ) or  $\text{Y}^{3+}$  ( $\text{O}_h(\text{Y})$ ). The structures represent the central  $\text{Pr}^{3+}$  ion (grey) surrounded by eight  $\text{F}^-$  (green) and the second coordination sphere containing  $\text{Na}^+$  (yellow) or  $\text{Y}^{3+}$  (blue). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

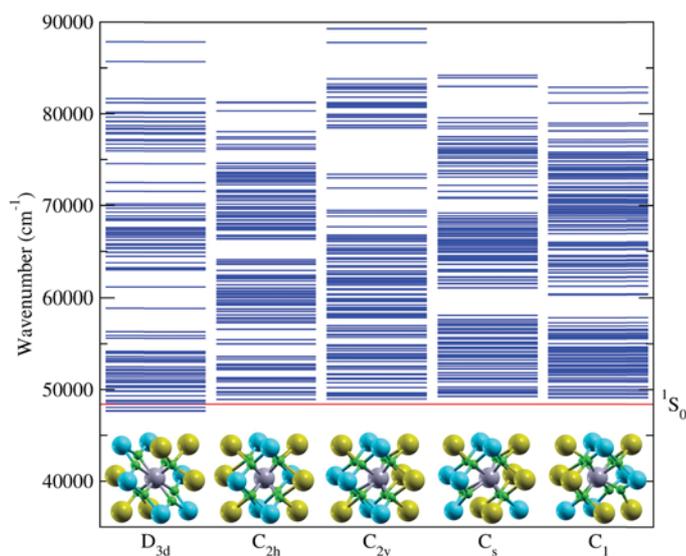
still located at about  $47\,000\text{ cm}^{-1}$  (see Figure 1 and 3). Therefore, the lowest energy level of the  $[\text{Xe}]4f^1 5d^1$  configuration is located above the highest energy level  $^1\text{S}_0$  which means that PCE for this phosphor is present. The emission spectrum of  $\alpha\text{-NaYF}_4:\text{Pr}^{3+}$  is dominated by sharp intraconfigurational  $[\text{Xe}]4f^2-[\text{Xe}]4f^2$  transitions which is in good agreement with previous results of Sommerdijk et al.

[18]. The emission lines in the UV part of the spectral range originate from the  $^1\text{S}_0$  energy level with the maximum at  $24\,600\text{ cm}^{-1}$  due to the  $^1\text{S}_0-^1\text{I}_6$  transition and representing the first photon. The emission lines in the visible part of the spectral range originate from the  $^3\text{P}_0$  energy level and representing the second photon. In the UV range at around  $43\,500\text{ cm}^{-1}$  there is a small amount of broad emission which cannot be assigned to any  $[\text{Xe}]4f^2-[\text{Xe}]4f^2$  transition known for  $\text{Pr}^{3+}$  and which was already described elsewhere [19]. This could lead back to a small amount of interconfigurational  $[\text{Xe}]4f^1 5d^1-[\text{Xe}]4f^2$  emission originating from the lowest energy level of the  $[\text{Xe}]4f^1 5d^1$  configuration. In contrary to  $\text{LaPO}_4:\text{Pr}^{3+}$  where the combination of sharp intraconfigurational  $[\text{Xe}]4f^2-[\text{Xe}]4f^2$  transitions and broad interconfigurational  $[\text{Xe}]4f^1 5d^1-[\text{Xe}]4f^2$  transitions is only observed at low temperatures [38] here this is already occurs at room temperature.

To explain the differences between the above given theoretical results (see Figure 3) and the experimental measurements (see Figure 4), new models were performed assuming a distortion of the  $\text{O}_h$  symmetry [39]. This distortion originates from the second coordination sphere of  $\text{Pr}^{3+}$  which consists of 12 sites randomly occupied by  $\text{Na}^+$  (132 pm) and  $\text{Y}^{3+}$  (116 pm). Unlike as mentioned in [40] the second coordination sphere is affecting the anions which are then responsible for the change of the ligand field. Since the ionic radii as well as the ionic charge of these two ions are so different distortion of the symmetry is expected. Taking into account the second coordination sphere,  $2^{12} = 4096$  different structural conformations are possible, from which only two extreme situations exhibit  $\text{O}_h$  symmetry. Due to the large number of structural conformations, here we analyze only the situation where the second coordination sphere contains exactly 6  $\text{Na}^+$  and 6  $\text{Y}^{3+}$  ions beside the two extreme situations discussed before (for more information see Section 4). The model parameters of the  $\text{O}_h$  cases (see Table 1) are modified for the distorted conformations using the AOM for the angular distortion and DFT for the radial part. Thus the descent in symmetry goes from  $\text{D}_{3d}$  to only  $\text{C}_1$ . The results of these calculations are given in Figure 5.



**Figure 4.** Room temperature luminescence spectra of  $\alpha\text{-NaYF}_4:\text{Pr}^{3+}$  (1.0%). VUV excitation spectrum is given on the left and emission spectrum on the right. The dashed grey line represents the energy position of the  $^1\text{S}_0$  energy level.



**Figure 5.** Calculated multiplet energy levels of the  $[Xe]4f^1 5d^1$  configurations of the  $Pr^{3+}$  doped  $\alpha$ - $NaYF_4$  in different symmetries. The solid red line characterizes the energy of the  $^1S_0$  energy level of the ground  $[Xe]4f^2$  configuration. The structures represent the central  $Pr^{3+}$  ion (grey) surrounded by eight  $F^-$  (green) and the second coordination sphere containing  $Na^+$  (yellow) and  $Y^{3+}$  (blue). (For interpretation of the references to colour in this figure legend, the reader is referred to the web version of this article.)

The multiplet energy levels arising from the  $[Xe]4f^2$  configurations is not presented in Figure 5, since the influence of the chemical surrounding is very low. The influence of the chemical surrounding on the 5d orbitals for the given symmetries is much stronger which results for each case in a different splitting. Therefore, we achieve symmetries where the lowest energy level of the  $[Xe]4f^1 5d^1$  configuration is located below the highest energy level  $^1S_0$  and do not show PCE like  $D_{3d}$ . However, for symmetries viz.  $C_{2h}$ ,  $C_{2v}$ ,  $C_s$ , and  $C_1$  the lowest energy level of the  $[Xe]4f^1 5d^1$  configuration is located above the highest energy level  $^1S_0$  which leads to PCE (see Figure 5). Notice that lower symmetry structures would also be more common among the 4096 different structural configurations than higher ones. This explains the PCE process in  $\alpha$ - $NaYF_4$  as an effect of lowering the symmetry due to the effect of the second coordination sphere, as well as the small amount of interconfigurational  $[Xe]4f^1 5d^1 - [Xe]4f^2$  emission, which would come from  $Pr^{3+}$  ions occupying higher symmetry sites.

### 3. Conclusions

In summary, the alkaline earth fluorides, ( $CaF_2$ ,  $SrF_2$  and  $BaF_2$ ) do not show PCE since the  $Pr^{3+}$  is located at a crystallographic position with  $O_h$  symmetry. The splitting of the 5d orbitals in this symmetry is larger, insofar as the lowest energy level of the  $[Xe]4f^1 5d^1$  configuration is always located below the highest energy level  $^1S_0$  of the ground  $[Xe]4f^2$  configuration. Our calculations fit to the experimental data, which show mainly interconfigurational  $[Xe]4f^1 5d^1 - [Xe]4f^2$  emission.  $\alpha$ - $NaYF_4$  offers as well  $O_h$  symmetry for the cation position. The calculation of such a system where the  $Pr^{3+}$  is located at a crystallographic position with  $O_h$  symmetry would lead to a material without showing PCE. This is in contradiction with the experimental data which show mainly intraconfigurational  $[Xe]4f^2 - [Xe]4f^2$  emission lines. By lowering the symmetry starting from a high  $D_{3d}$  to the low  $C_1$  this extraordinary finding can be explained. The lower symmetries which describe a distortion of the crystallographic position can be easily explained by the second coordination sphere. Moreover, with these different symmetries it is possible to explain the emission

spectra which shows in addition a small part of interconfigurational  $[Xe]4f^1 5d^1 - [Xe]4f^2$  transitions in the UV part of the spectral range.

## 4. Experimental

### 4.1. Computational details

VASP calculations were performed to determine the surrounding structure of  $Pr^{3+}$  in a periodic lattice. PBE functional was used for the exchange-correlation potential. The Projector Augmented Wave method (PAW) was used to reproduce the interaction of the valence electrons with the nuclei and core electrons. A plane-wave basis set with a cutoff energy of 400 eV was used to reproduce the electronic states. The atomic positions were relaxed until all forces were smaller than 0.001 eV/Å. From the relaxed structure, molecular calculations were performed with ADF 2013.01 to obtain the electrostatic and ligand field parameters. A TZ2P+ basis set was used for Pr, and a TZP basis set was used for F. Point charges are included at the distance of the  $Pr^{3+}$  second coordination sphere to reproduce the effect of the lattice potential. The distorted structures of  $NaYF_4$  are obtained from molecular calculations by fixing the positions of the  $Na^+$  and  $Y^{3+}$  ions in the second sphere, allowing to relax the  $Pr^{3+}$  and  $F^-$  ions.

### 4.2. Experimental details

All phosphors were prepared by precipitation from aqueous solution at the Department of Chemical Engineering, Münster University of Applied Sciences. The concentration of  $Pr^{3+}$  in the so prepared phosphors was adjusted to 1%.

In case of the alkaline earth fluorides the alkaline earth nitrates, viz.  $Ca(NO_3)_2 \cdot 4H_2O$  (ProAnalyti, Merck),  $Sr(NO_3)_2$ , (ProAnalyti, Merck), and  $Ba(NO_3)_2$ , (ProAnalyti, Merck), were dissolved in water together with stoichiometric amounts of  $Pr(NO_3)_3 \cdot 6H_2O$  (99.9%, Alfa Aesar) and subsequent dropwise addition of dissolved  $NH_4HF_2$  (95%, Alfa Aesar) until precipitation occurred. After filtration and drying 1% NaF was added for charge compensation. The mixtures were then filled into glassy-carbon crucibles and sintered for 6 h at 900 °C in a nitrogen stream. The nitrogen, which was used to avoid the reaction of the fluorides with oxygen, was further purified by drying with molecular sieve and KOH.

For the  $\alpha$ - $NaYF_4$  a stoichiometric mixture of  $YCl_3 \cdot 6H_2O$  (99.9%, Treibacher Industrie AG) and  $PrCl_3 \cdot 6H_2O$  (99.9%, Sigma-Aldrich) was dissolved in water and combined with a solution of a ten times molar excess of NaF (ProAnalyti, Merck). Precipitation occurred immediately and after filtration and drying the mixture was filled into a glassy-carbon crucible and sintered for 6 h at 600 °C in a nitrogen stream. This temperature was chosen to avoid the transformation of the cubic  $\alpha$ -phase of  $NaYF_4$  to the hexagonal  $\beta$ -phase.

### 4.3. Characterization

All luminescence measurements were performed at the Department of Chemical Engineering, Münster University of Applied Sciences.

For all luminescence measurements the powder samples were pressed into a PTFE-sample holder, whereby the surface was structured by using a white fleece afterwards. All investigated powder samples were excited at 160 nm and the luminescence spectra recorded with a VUV spectrometer (Edinburgh Instruments FS920). The spectrometer was equipped with a VUV monochromator VM504 from Acton Research Corporation (ARC) and a deuterium lamp as an excitation source. The sample chamber was flushed with dried Nitrogen in order to prevent absorption of VUV radiation by water and oxygen. Excitation and emission spectra were recorded in the ranges of 120–250 nm and 200–800 nm, respectively. The

emission spectra were corrected by using a correction file obtained from a tungsten incandescent lamp certified by NPL. The relative VUV excitation intensities of the samples were corrected by dividing the measured excitation spectra of the samples with the excitation spectrum of sodium salicylate ( $\text{o-C}_6\text{H}_4\text{OHCOONa}$ ) under the same excitation conditions. The measurements were performed at ambient temperature and pressure with a step size of 0.5 nm.

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