

## Brushlike Interactions between Thermoresponsive Microgel Particles

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Using a simplified microstructural picture we show that interactions between thermosensitive microgel particles can be described by a polymer brushlike corona decorating the dense core. The softness of the potential is set by the relative thickness  $L_0$  of the compliant corona with respect to the overall size of the swollen particle  $R$ . The elastic modulus in quenched solid phases derived from the potential is found to be in excellent agreement with diffusing wave spectroscopy data and mechanical rheometry. Our model thus provides design rules for the microgel architecture and opens a route to tailor rheological properties of pasty materials.

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Thermoresponsive microgel particles are a hybrid between a colloidal and a polymeric system with properties that can be tuned externally [1–3]. Most of the previously studied stimuli responsive microgel systems are based on poly(*N*-isopropyl-acrylamide) (PNIPAM), a polymer which has a lower critical solution temperature (LCST) of approximately 33 °C [1]. Above the LCST, the microgel particles expel water and are collapsed. The typical size of a collapsed microgel particle is in the range of 0.2–1  $\mu\text{m}$ . Upon lowering the temperature the particles swell to about twice their original size. Responsive microgels thus provide the possibility to fabricate *smart* colloidal materials for applications as viscosity modifiers, carrier systems, bioseparators, optical switches, or sensors [1,2,4]. Moreover, due to their tunability they are ideal model systems to study the phase behavior, glass transition, and jamming in dense colloidal dispersions [5–7].

Particles come into contact and form a viscoelastic paste below the LCST if the polymer density inside the swollen particles approaches the total polymer density. A number of rheological studies have revealed the apparent divergence of the viscosity at the transition point and the emergence of an elastic shear modulus [2,3]. Since the particles consist of polymers and solvent in equilibrium, they are elastically compliant, and thus elastic moduli do not diverge at the jamming transition, unlike the behavior of rigid colloidal particles [7,8]. Several experimental studies show that in this regime the bulk modulus as a function of the effective volume fraction scales as a power law  $G_p \propto \phi_{\text{eff}}^{1+n/3}$  with values of  $n$  ranging from  $n = 9$  to  $n = 22$  [2,3]. These findings indicate that the particle interaction potential  $\psi(r) \propto r^{-n}$  also follows a power law, at least over some significant range of length scales [2,3]. Unfortunately, a detailed model for the origin of these interactions has been missing. This is mainly due to the fact that modeling the interaction between swollen particles is complicated by the heterogeneous microstructure arising from

the faster reaction rate of cross-linking compared to polymerization [9]. In this Letter we show that interactions between thermosensitive microgel particles can be modeled by a polymer brushlike corona decorating the dense core [10–12]. The softness of the potential is set by the relative thickness of the compliant corona with respect to the overall size of the swollen particle.

Our PNIPAM microgel particles have been synthesized by standard methods and characterized as described in Ref. [13]. The high cross-linker to monomer ratio of 5.3 mol % *N,N'*-methylene-bis-acrylamide (BIS) leads to relatively rigid microgel cores with, on average, one molecule of cross-linker per 19 molecules of NIPAM monomer. In Fig. 1 we show the temperature dependence of the hydrodynamic radius  $R_H$  determined by dynamic light scattering. The particle radius in the collapsed state is  $R_0 \approx 250$  nm for which the internal polymer volume fraction is

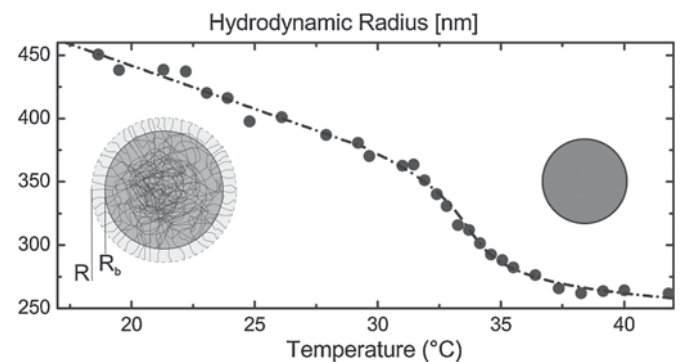


FIG. 1. PNIPAM hydrodynamic radius  $R_H$  as obtained from dynamic light scattering. Dash-dotted line shows the interpolation curve used to calculate the effective volume fraction  $\Phi_{\text{eff}} \propto R_H^3$ . The sketch (drawn to scale) illustrates the swelling of the particles: Our experiments suggest that the particles consist of a highly cross-linked core with radius  $R_b$  and a corona of uncross-linked polymer chains that can swell to a brush of thickness  $L_0 \approx R - R_b$  under good solvent conditions (left).

approximately  $\phi_0 \approx 70\%$  [13]. For  $T = 20^\circ\text{C}$  the particles reach a hydrodynamic radius of  $R_H = 440$  nm, almost doubling their size. As particles swell they acquire a radially inhomogeneous density profile. While the exact density distribution  $\phi(\rho)$  in the swollen state remains unknown, scattering experiments clearly indicate the presence of a moderately swollen core and a highly swollen corona [3,13–15]. For our particles we find from static light scattering a polymer density of  $\phi \approx 35\%$  in the core and  $\phi < 10\%$  in the corona (at  $\rho > 0.8R_H$ ) [13]. Classical Flory-Rehner theory [15,16] for swollen polymer gels provides estimates for the degree of polymerization between cross-links  $N_c$  in the core and corona regions. Using literature data for the statistical segment length  $a \approx 0.81$  nm [17] and the Flory interaction parameter  $\chi$  [18] of NIPAM, we find  $N_c \sim 10$  in the core of the particle, in agreement with the stoichiometry of the microgel synthesis. Moreover, for typical corona densities we find  $N_c \gg 100$ , suggesting an essentially uncross-linked corona region for our polymerization conditions.

Below the LCST these corona chains extend into the good solvent and form a swollen brushlike layer of thickness  $L_0$ . While the transition between the core and corona regions is not an abrupt one, we adopt the simplified scaling picture of Alexander [10] of the brush as a collection of identical chains of length  $N$  grafted at moderate-to-high surface density to a reference surface at  $\rho = R_b$ . In good solvent conditions, the thickness of such a brush scales as  $L_0 \sim Ns^{-2/3}a^{5/3}$ , where  $s \sim a\phi_b^{-3/4}$  is the average separation between grafting sites. Note that other more realistic models also predict  $L_0 \sim N$  [11], so the simplicity of our model should not adversely affect the results at the scaling level. Results from static light scattering indicate typical values of  $\phi_b \sim 3\%$  and  $L_0 \sim 100$  nm for our particles [13]. From these values we can estimate  $s \sim 10$  nm and  $N \sim 700$ . This means the corona density is well above the overlap concentration  $\phi^* \approx N^{-4/5}$  and  $s < L_0$  which shows the consistency of our arguments.

We note that due to the high degree of cross-linking the stiffness of the core region is substantially higher than the soft brushlike corona [16]. More generally, as long as the number of monomers between cross-links is less than the number of monomers in a corona chain, the core will be less compliant than the corona region. As we are well within this regime, we may treat the core as an effectively incompressible solid for the weak to moderate particle deformations considered. Here, the choice of a reference surface,  $R_b$ , is somewhat arbitrary but should reflect the boundary between core and corona behavior.

We now turn our attention to the properties of a dense microgel assembly with a total polymer concentration of about 135 mg/ml [13]. From laser scanning confocal microscopy studies of a diluted sample we determined the particle number density of the dense system to be  $\eta = 2.24/\mu\text{m}^3 \pm 2\%$ . Over the range of temperatures covered, the effective particle volume fraction  $\Phi_{\text{eff}}$  thus increases

from about 0.2 to 0.9. We use two-cell diffusing wave spectroscopy (DWS) in the transmission geometry to study particle diffusion, dynamical arrest, and buildup of elasticity [19]. DWS, dynamic light scattering in the highly multiple-scattering limit, provides information on the thermally induced fluctuations of the microgel particles on the nanoscale via the temporal intensity autocorrelation function  $g_2(t)$  of multiply scattered light. In particular, the ensemble-averaged mean square displacement (MSD),  $\langle \Delta r^2(t) \rangle$ , can be extracted from  $g_2(t)$ . Details of the setup can be found in Ref. [20]. The sample is kept in a glass cuvette with inner dimensions  $10 \times 2$  mm (Hellma, Germany). To avoid crystallization the sample is loaded hot, quenched below  $20^\circ\text{C}$ , and subsequently the temperature is increased in steps of  $0.5^\circ\text{C}$  or  $1^\circ\text{C}$ . At each temperature the sample is kept for about 10 min to equilibrate and  $g_2(t)$  is recorded over an additional 10 min. For our microgel suspensions,  $g_2(t)$  (partially) relaxes in a characteristic time  $\tau$  that depends on temperature. In the case of more dilute suspensions,  $g_2(t)$  exhibits a roughly exponential decay characteristic of simple diffusion, with  $\langle \Delta r^2(t) \rangle = 6D_s(\phi)t$ . However, for concentrated suspensions, the behavior is more complex. At temperatures between  $27^\circ\text{C}$  and  $30^\circ\text{C}$ ,  $g_2(t)$  exhibits a slightly stretched exponential decay and a corresponding power-law MSD,  $\langle \Delta r^2(t) \rangle \sim t^\beta$  with  $\beta \lesssim 1$ , characteristic of a crowded suspension of soft, repulsive particles.

However, at  $T = 27^\circ\text{C}$  and below the particles have swollen into contact and the short-time decay of  $g_2(t)$  is only a partial one, leading to a plateau value of the MSD characteristic of the elastic properties of the jammed suspension [21]. Figure 2 shows plots of  $\langle \Delta r^2(t) \rangle$  versus time  $t$  for a range of temperatures above and below the jamming transition.

We first analyze the influence of crowding on the temperature dependence of the self-diffusion coefficient  $D_s(\phi)$  for  $T \geq 30^\circ\text{C}$ . As shown in Fig. 3 our results are well described by the semiempirical expression of Lionberger and Russel for hard spheres [22]:  $D_0/D_s(\Phi_{\text{eff}}) = [(1 - 1.56\Phi_{\text{eff}})(1 - 0.27\Phi_{\text{eff}})]^{-1}$ , where  $\Phi_{\text{eff}} = \eta \times 4\pi R^3/3$ .

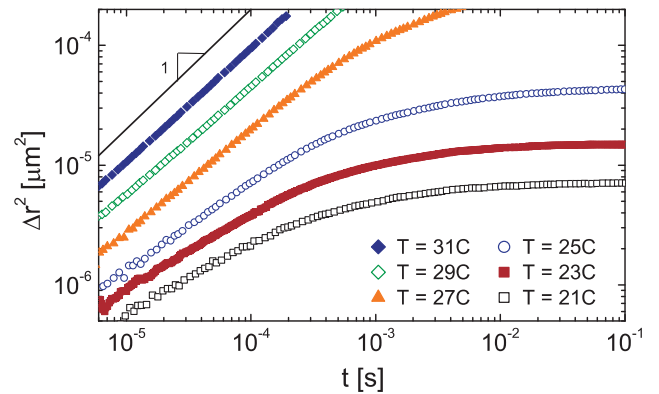


FIG. 2 (color online). Thermally activated nanoscale motion. Mean square displacement  $\langle \Delta r^2(t) \rangle$  of the microgel particles from diffusing wave spectroscopy.

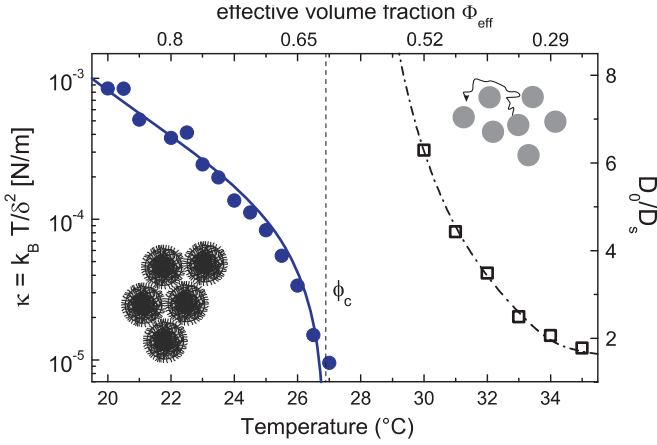


FIG. 3 (color online). Microgel liquid-solid transition as a function of temperature. The transition is driven by the change in effective particle volume due to swelling. The reciprocal short-time diffusion coefficient  $D_0/D_s$  (open squares) increases strongly when approaching the transition. Dash-dotted line: semiempirical expression by Lionberger and Russel for hard spheres. Solid circles: elastic spring constant  $\kappa = k_B T / \delta^2$  from DWS. Solid line is calculated from Eq. (3) with ( $\Phi_c = 0.625$ ,  $\alpha = R_b/R = 0.8$ ).

Here we have introduced an effective steric radius  $R = R_H \times 1.027$  that reflects quantitatively the hard-sphere-like behavior in the liquid state.

At temperatures 27 °C and below, where the system has entered a viscoelastic solid phase, the swollen particles are trapped and the assembly is dynamically arrested. We know that in the swollen state the particle's mass is primarily concentrated in a sphere of size  $R_b$ , whereas the dynamic properties are governed by the effective size  $R$  which includes a compliant corona,  $R \approx R_b + L_0$ . We can therefore consider the thermal motion of the particle core, radius  $R_b$ , as a probe of the particle interactions defined by the quenched particle coronas. The particle MSD shown in Fig. 2 clearly indicates a plateau value at long times. From equipartition of energy, a local spring constant can be defined by the maximum value  $\delta^2$  of the MSD in the plateau region,  $\kappa \approx kT/\delta^2$ , which can be directly related to the interaction potential  $\psi$  between two spheres  $\kappa = \partial^2 \psi / \partial r^2$ . In Fig. 3 we show the temperature dependence of  $\kappa$  in the arrested state, determined from the mean square displacement at  $t \sim 0.1$  s.

As outlined above we propose that the particle corona can be modeled as a polymer brush of thickness  $L_0$  [10,11] that extends into the good solvent from a reference surface located at  $R_b$ . Since typically  $L_0 \ll R_b$  curvature effects on the brush configuration and the particle interaction potential should be small. Thus the force between two particles separated by  $r = 2R_b + d$  may be written in the Derjaguin approximation [23,24] as

$$F(d) = \pi R_b \int_{2L_0}^d f(x) dx, \quad (1)$$

where  $f(d)$  is the force per unit area between two flat

surfaces [25]. The Alexander–de Gennes scaling model [10] predicts an  $f(d)$  of the form

$$f(d) \sim k_B T / s^3 [(2L_0/d)^{9/4} - (d/2L_0)^{3/4}], \quad (2)$$

with an unknown prefactor of order 1. The first term in Eq. (2) is set by the osmotic repulsion of a semidilute solution of equal density whereas the second term is the chain tension due to the entropic penalty upon stretching the grafted chains. The spring constant is thus  $\kappa = \partial F(d)/\partial d = \pi R_b f(d)$ . Defining a characteristic ratio  $\alpha = R_b/R < 1$  we can replace  $d/2L_0$  by  $(r/R - 2\alpha)/(2 - 2\alpha)$  [26]. We can now write the spring constant in terms of the reduced volume fraction  $\tilde{\Phi} = \Phi_{\text{eff}}/\Phi_c$  since  $r/R \approx 2\tilde{\Phi}^{-1/3}$ . For random close packing conditions,  $\Phi_c \approx 0.64$ . Note that at initial contact,  $r = 2R$ , we recover the liquid-to-solid transition. For simplicity we neglect the weak temperature dependence of  $R_b$  and find:

$$\kappa \propto \left( \frac{1 - \alpha}{\tilde{\Phi}^{-1/3} - \alpha} \right)^{9/4} - \left( \frac{\tilde{\Phi}^{-1/3} - \alpha}{1 - \alpha} \right)^{3/4}. \quad (3)$$

The spring constant directly sets the scale for the macroscopic shear modulus via  $\pi R G_p \sim \kappa$ . This can be obtained at a scaling level by equating the displacement energy  $\delta^2 R G_p$  with the thermal energy  $kT$ . For a multiparticle system, the same scaling relation can also be derived from the statistical mechanical theory of Zwanzig and Mountain [27,28]. Figures 3 and 4 show the excellent agreement of Eq. (3) with the DWS data using  $R_b/R = 0.8$  and  $\Phi_c = 0.625$ . To cover an even larger range of effective volume fractions we include in our analysis literature data of two well characterized microgel systems [3]. The two systems are similar to ours except for the lower amount of BIS

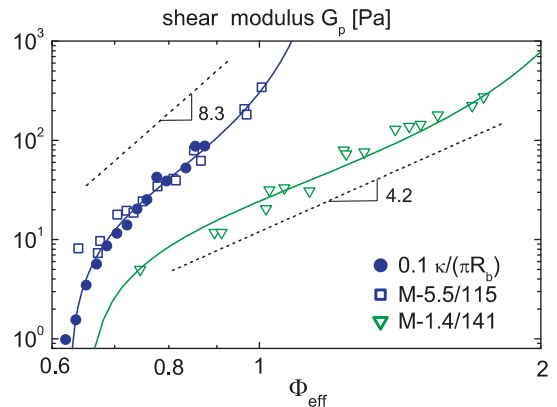


FIG. 4 (color online). Shear modulus of quenched microgels as a function packing density. Full symbols are derived from the diffusing wave spectroscopy data shown in Figs. 2 and 3. Open symbols: data reproduced from Ref. [3]. Squares (M-5.5/115): cross-linker concentration 5.5 mol% BIS and hydrodynamic radius  $R_H(25^\circ\text{C}) = 115$  nm. Open triangles (M-1.4/141): 1.4 mol% BIS and  $R_H(25^\circ\text{C}) = 141$  nm. Solid lines are calculated from Eq. (3) with ( $\Phi_c = 0.625$ ,  $\alpha = R_b/R = 0.8$ ) and ( $\Phi_c = 0.65$ ,  $\alpha = R_b/R = 0.63$ ). Dashed straight lines indicate a power-law scaling  $G_p \propto \Phi_{\text{eff}}^m$  with  $m = 1 + n/3$ .

cross-linker used for one of the systems. Interestingly the moduli of the highly cross-linked particles and our data can be collapsed on single curve, whereas the particles with a lower amount of cross-linker are substantially softer. Moreover, both the more rigid and the soft particle rheology can be described by our model. Note that, over a limited range of densities,  $G_p(\Phi_{\text{eff}})$  resembles a power law with an exponent  $m$  that depends strongly on  $\alpha = R_b/R$ .

In this work we have focused our attention on the general scaling concepts that govern the linear elasticity in microgel pastes. We showed that a simple polymer brush model captures the essential physics of the interparticle interactions, regardless of the various approximations made. Moreover, we were able to make detailed predictions for the bulk elastic modulus over a large range of effective volume fractions. Our results explain the origin of the power-law scaling of the elastic modulus in these systems, which emerges naturally as a consequence of interparticle interactions mediated by brushlike coronas of the microgel particle constituents. This simple picture should have broad utility for understanding the elastic properties of this important class of disordered soft solids.

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